

# 8<sup>o</sup> Seminario Internacional de Investigación

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**PISA 2015** | CARTAGENA DE INDIAS



## The efficiency of schools in an international comparison – results from PISA 2012

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# Agenda

- Research questions
- Data, descriptive statistics
- Results
  - Efficiency scores
  - Factors associated with efficiency scores
  - Efficiency and equity

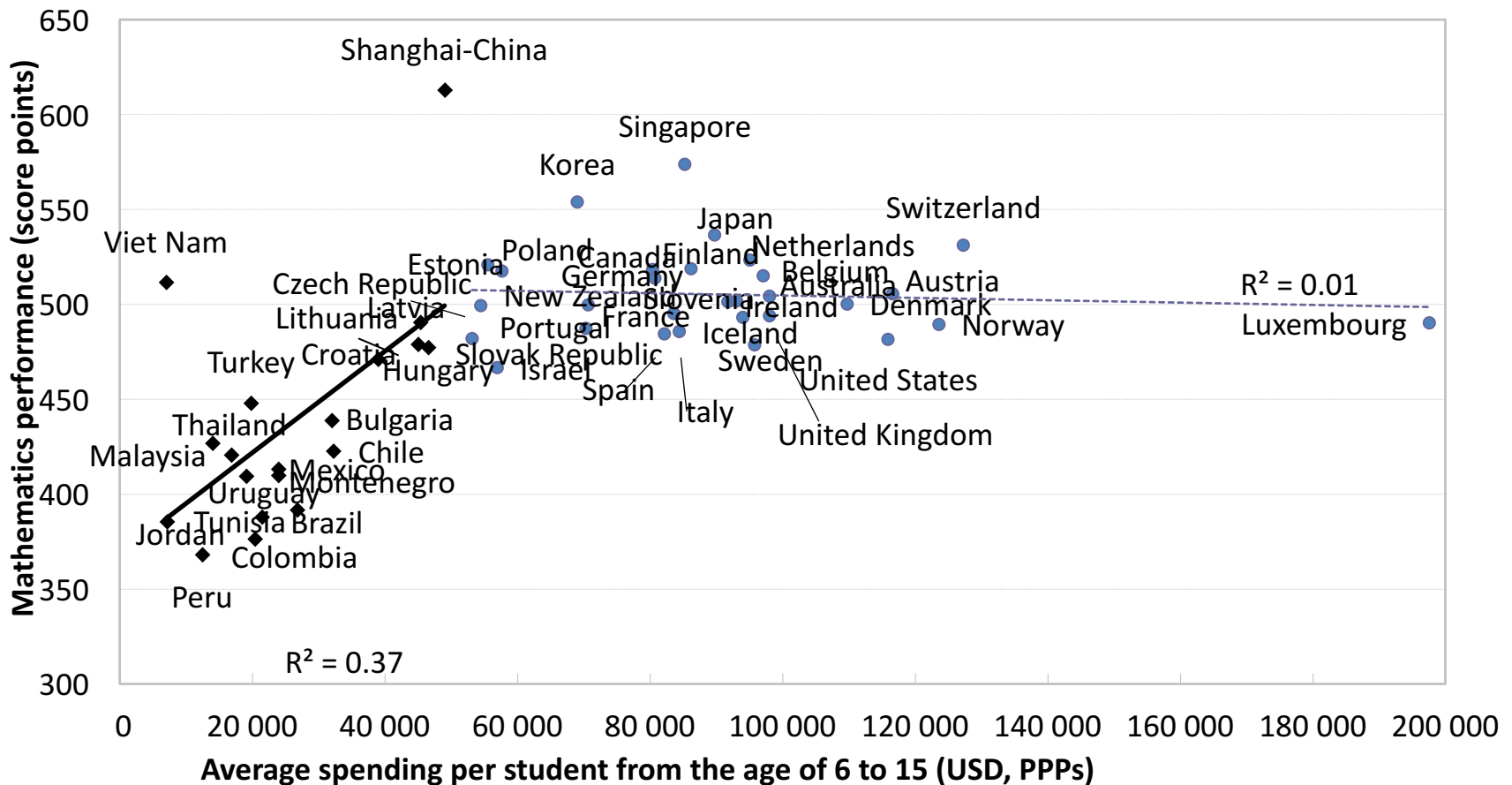
## Disclaimer

The author(s) received funding from the OECD Thomas J. Alexander fellowship program for carrying out this work. The work should not be reported as representing the official views of the OECD or of its member countries. The opinions expressed and arguments employed herein are those of the author(s).

## Research questions

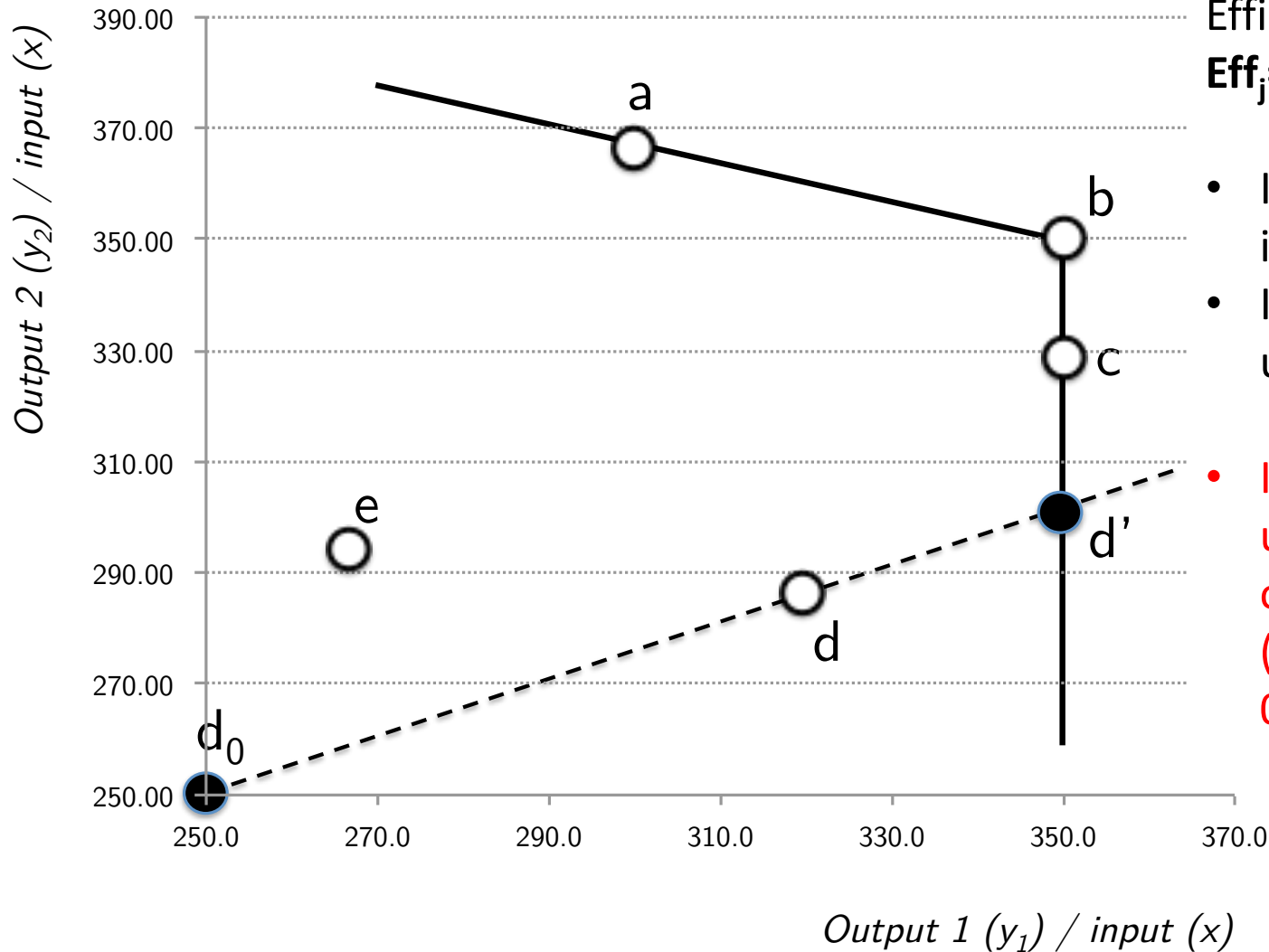
- How does the efficiency of schools in the high-spending countries look like, in a comparative perspective?
  - Are the differences between countries higher or lower than those within countries?
- Which are the main factors associated with the efficiency of schools, when estimated using an international benchmark?
  - Heterogeneity of these factors?
- How is the (eventual) link between schools' efficiency and equity?
  - Equality and/or inclusion

# Selection of countries



# Empirical model (1)

- Data Envelopment Analysis
  - Output orientation
  - Variable returns to scale (VRS)
  - Simar & Wilson (2000) bootstrap procedure (2,000 replicates) [estimated with Benchmarking © in R]
  - Robustness check:
    - SFA
    - DEA with different combinations of inputs and outputs
- Second-stage regression
  - Tobit regression
    - Robustness check: Simar & Wilson (2007) procedure



Efficiency score  
 $Eff_j = d_0 d' / d_0 d$

- If  $eff_j > 1$  is inefficient
- If  $eff_j = 1$  efficient unit
- In the paper I used the inverse of these scores (range between 0;1)

## Empirical model (3)

- Mathematically, DEA efficiency score is a ratio between (weighted) outputs and (weighted) inputs

$$\max \left( h_0 = \frac{\sum_{r=1}^s u_r y_{r0}}{\sum_{i=1}^m v_i x_{i0}} \right)$$

- $r(r=1,\dots,s)$  outputs and  $i(i=1,\dots,m)$  inputs;  $u$  and  $v$  are optimal weights
- Then, it is solved with linear programming

# Selection of inputs and outputs

- Literature, conceptual production function:
  - Quality/quantity of human and financial resources
  - *Expenditures – missing*
  - Students' socioeconomic background
  - Cognitive skills (i.e. test scores)
  - *Success in education (pass rates, graduation, etc.) – missing*
  - *Non-cognitive skills – missing [see extension]*
- Final selection
  - (Inverse of) students/teachers ratio (*St\_Ratio*)
  - Number of computers per student (*Computer\_n*)
  - Students' average *ESCS* (index of Economic, Social and Cultural Status)
  - Average test score in mathematics (*pv1math*) and reading (*pv1read*)

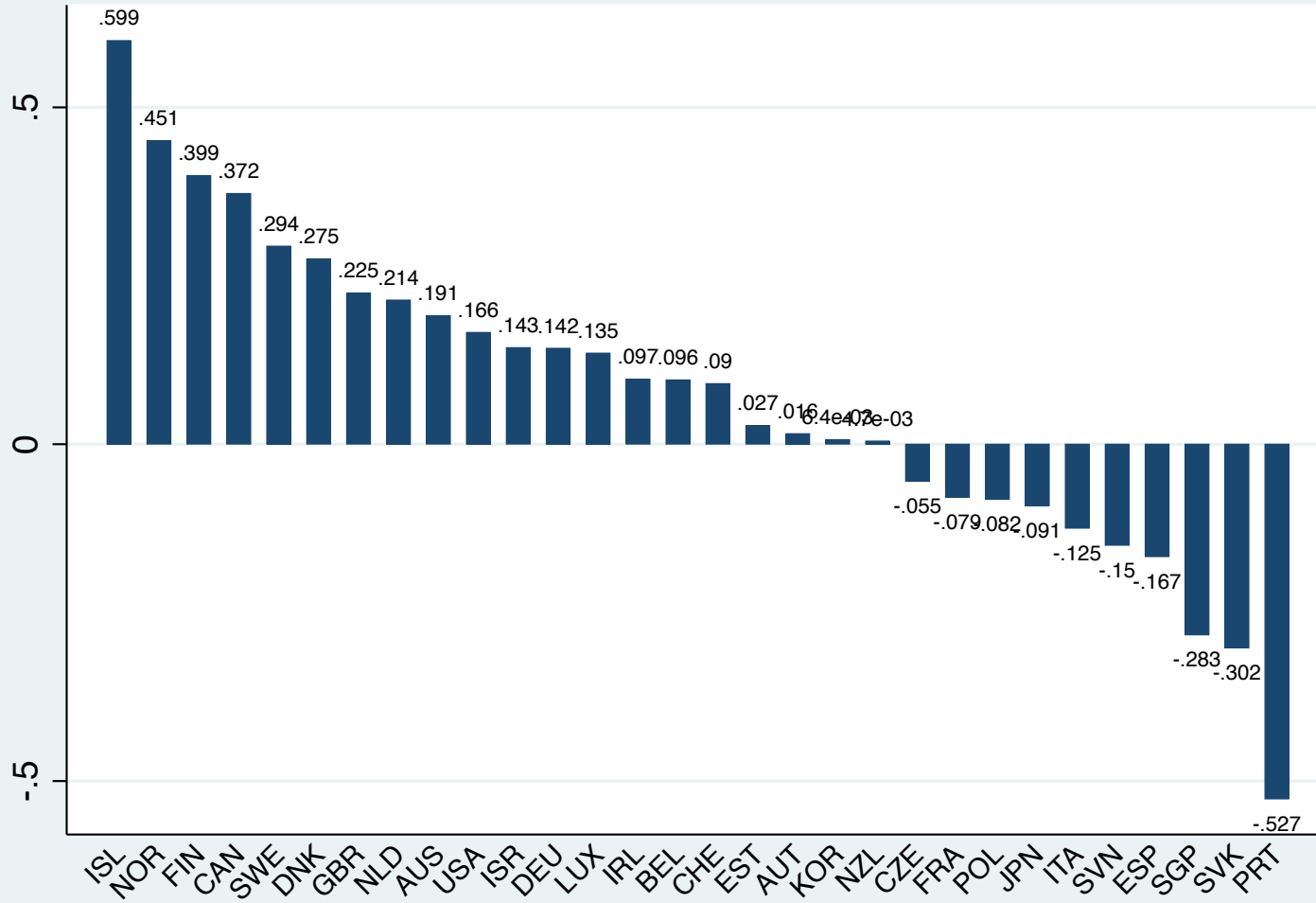


## Inputs and outputs, descriptive statistics

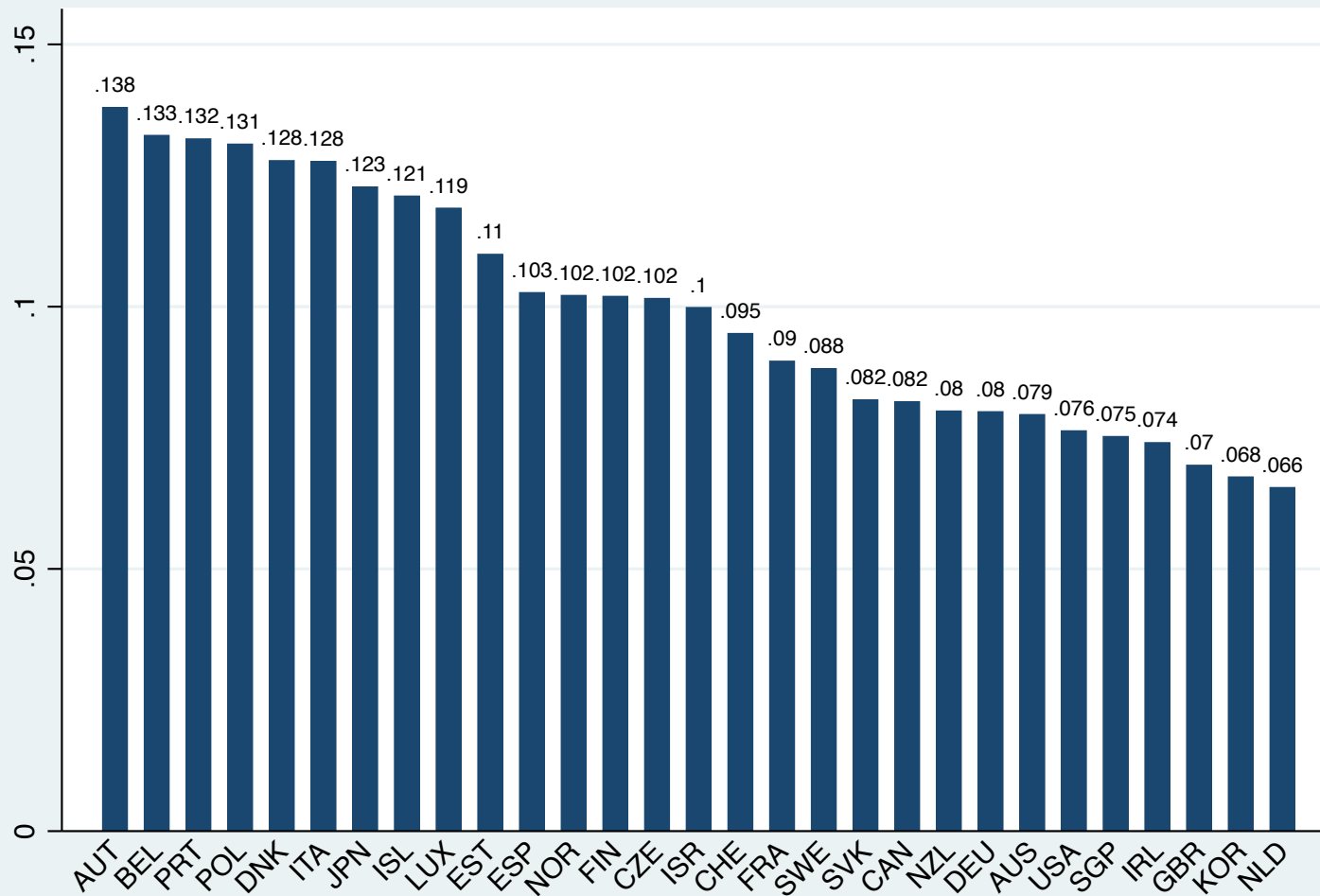
- In the overall sample: 8,640 schools

Variable	Mean	Std. Dev.
ESCS	0.063	0.528
StRatio	0.105	0.141
Computer_n	0.836	1.250
pv1math	496.583	63.736
pv1read	495.393	66.350

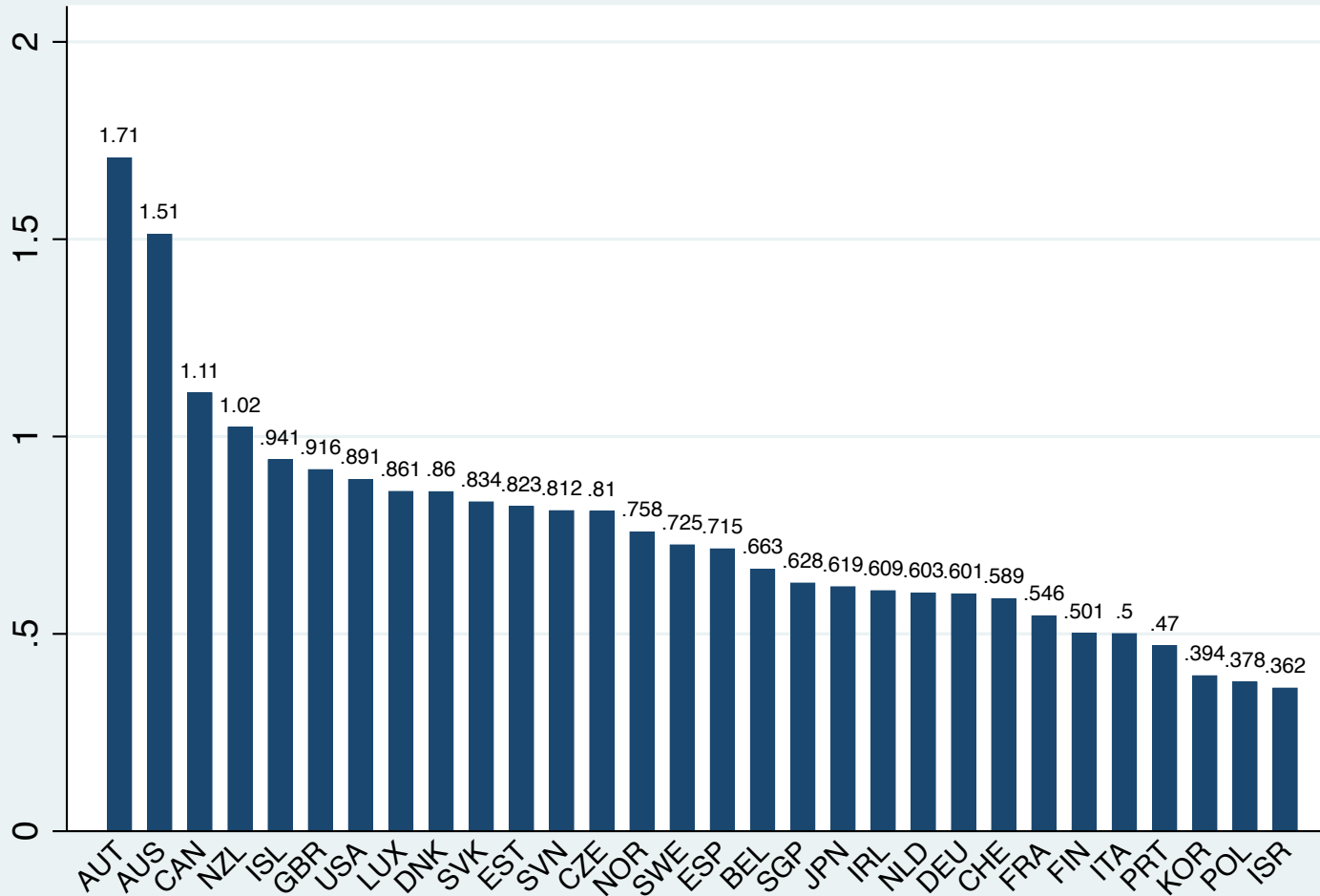
### Descriptive statistics, by country: ESCS



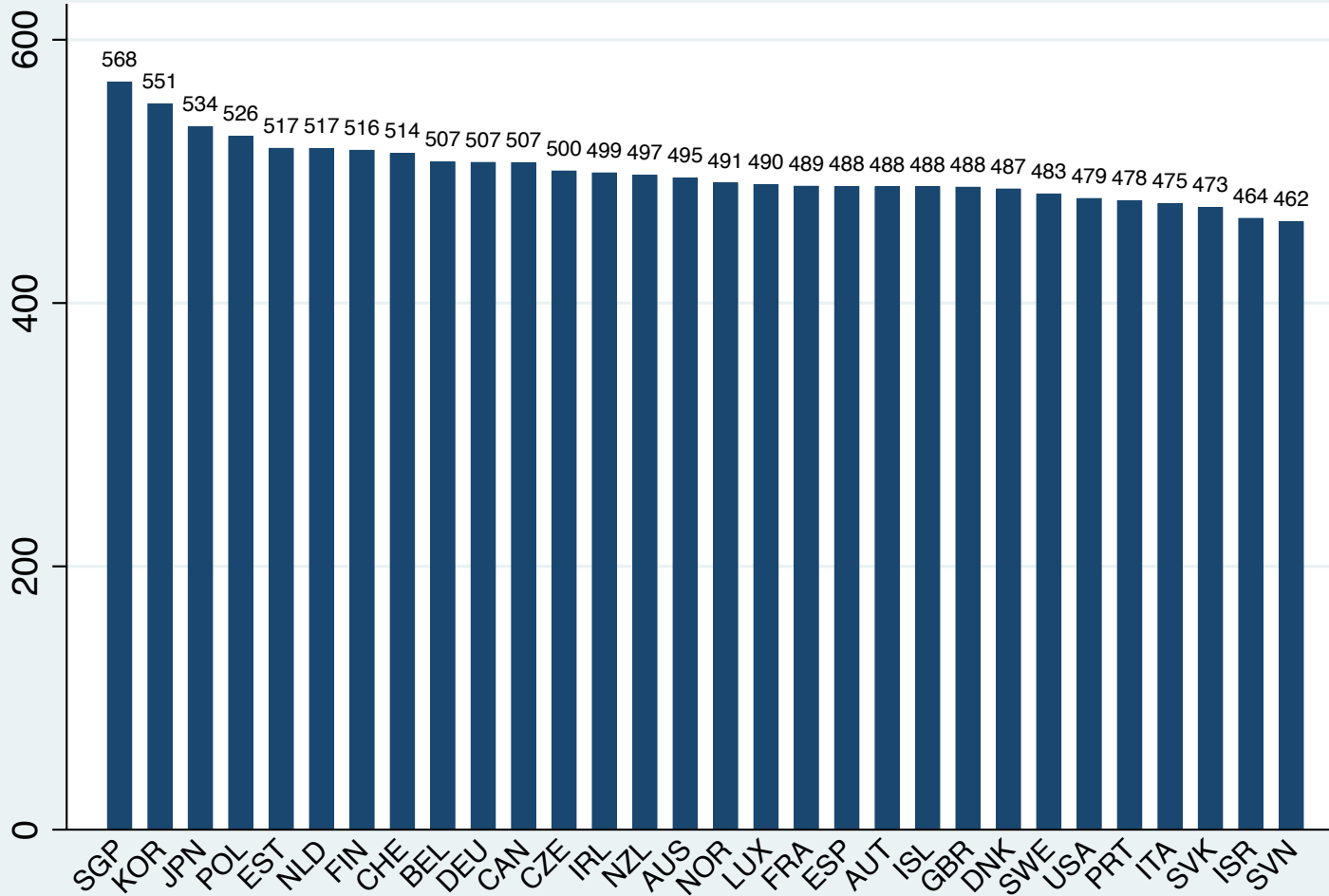
Descriptive statistics, by country: (inverse of) students/teachers ratio



Descriptive statistics, by country: # computers per student



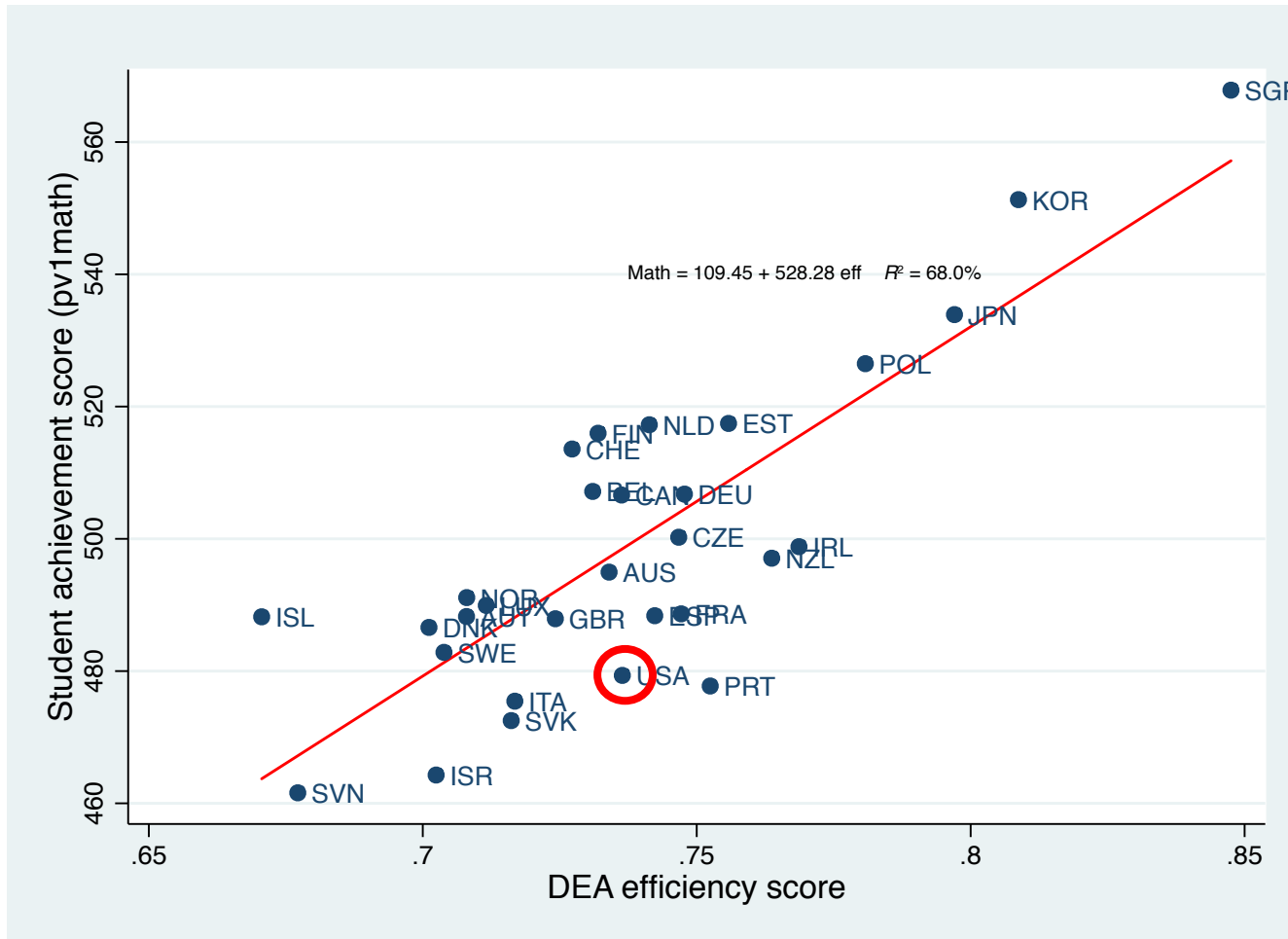
Descriptive statistics, by country: avg test score in mathematics



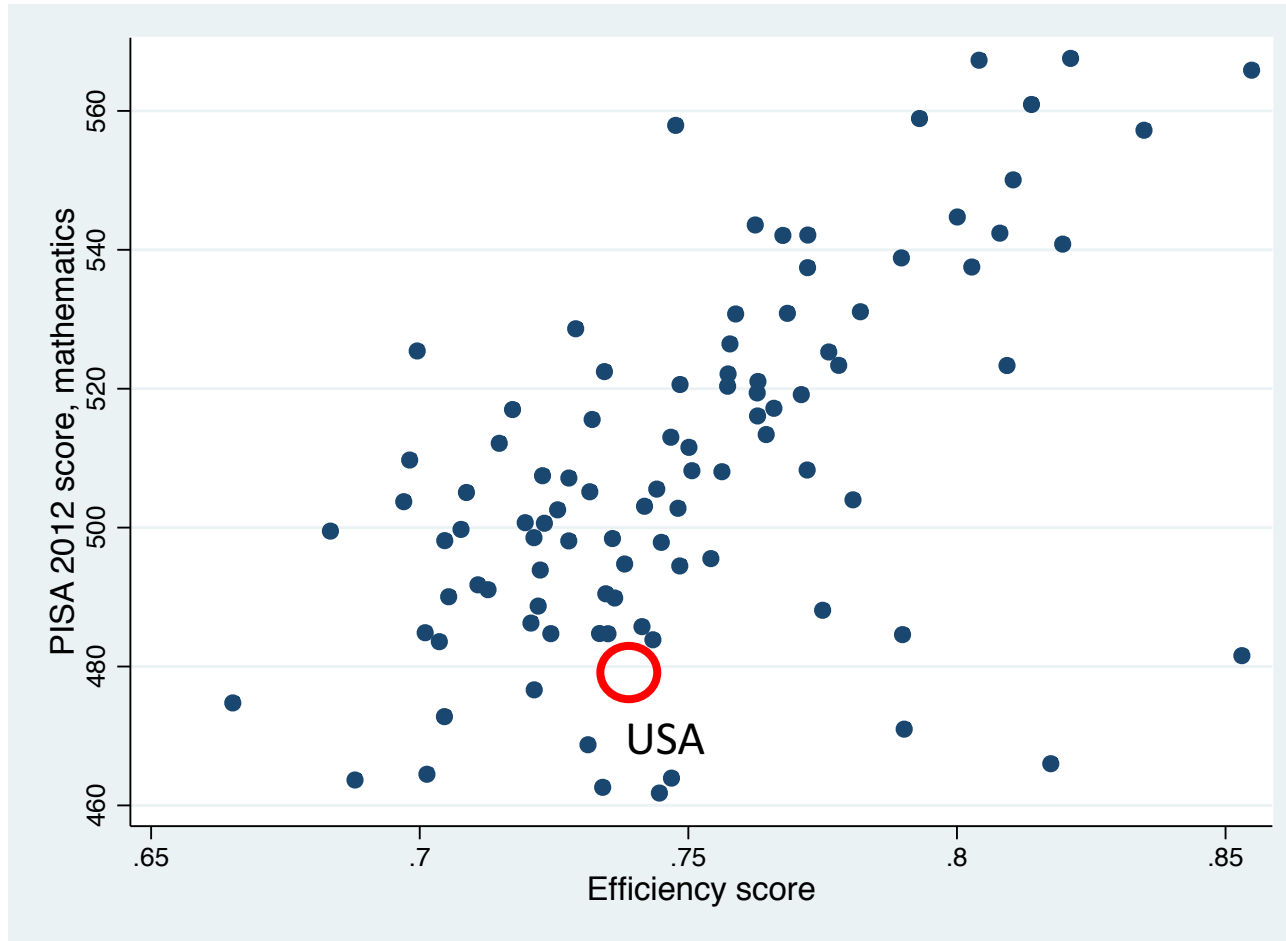
## Results: efficiency scores

- It is interesting to show not only mean schools' efficiency scores, but their **distribution by country**
  - How much differentiated are the educational systems, *within*?
  - How many schools are more efficient than the average – as computed through the international benchmark?
- There is NOT the “average” Italian, Spanish, American... etc. school
  - the main message: efficiency is a property of schools, not countries – the focus is not on structural differences
  - for the single school: the international benchmark allows a wider set of efficient solutions to look at for improving its own activities

# Efficiency and performance, by country

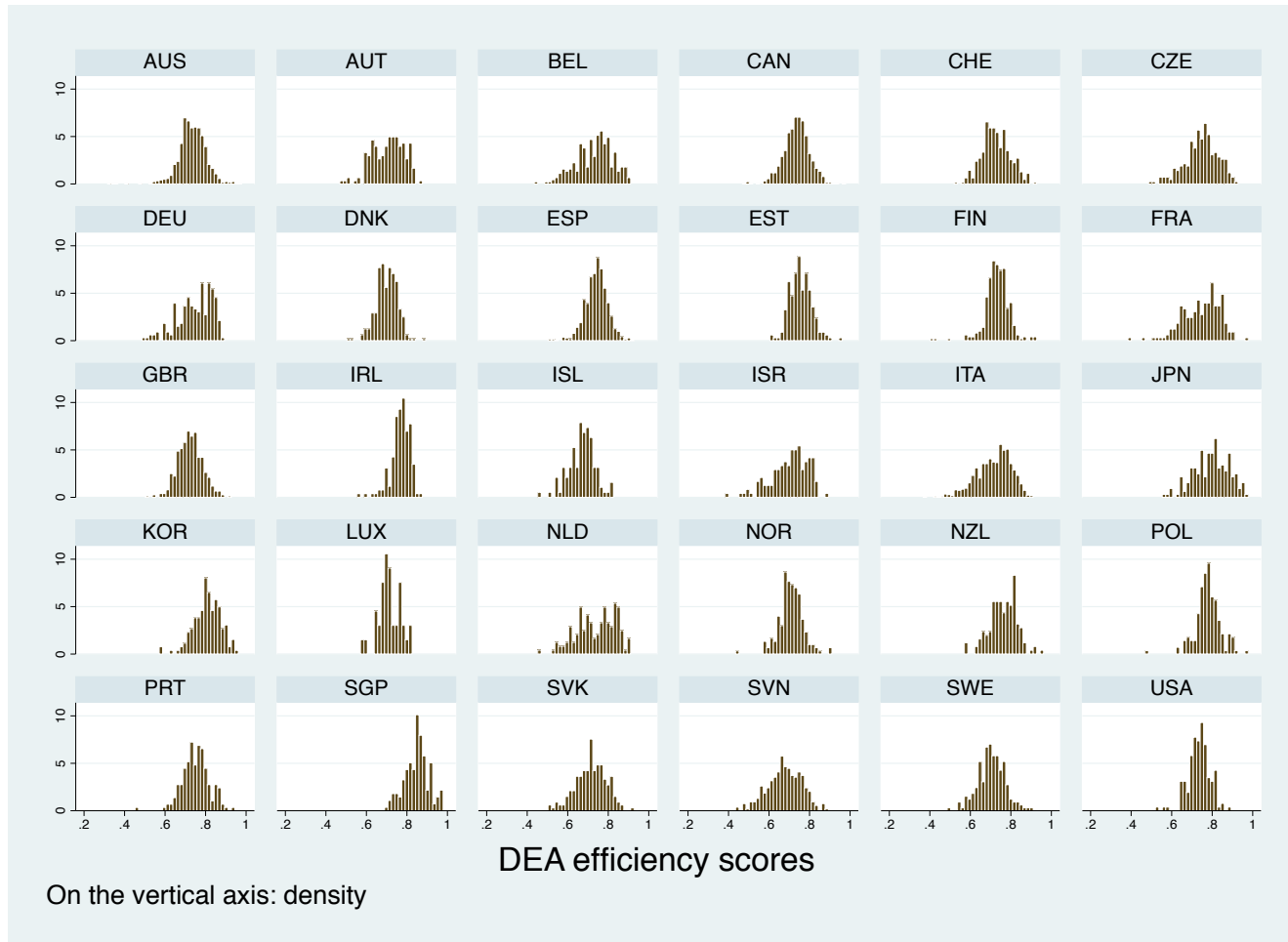


# Efficiency and performance: USA

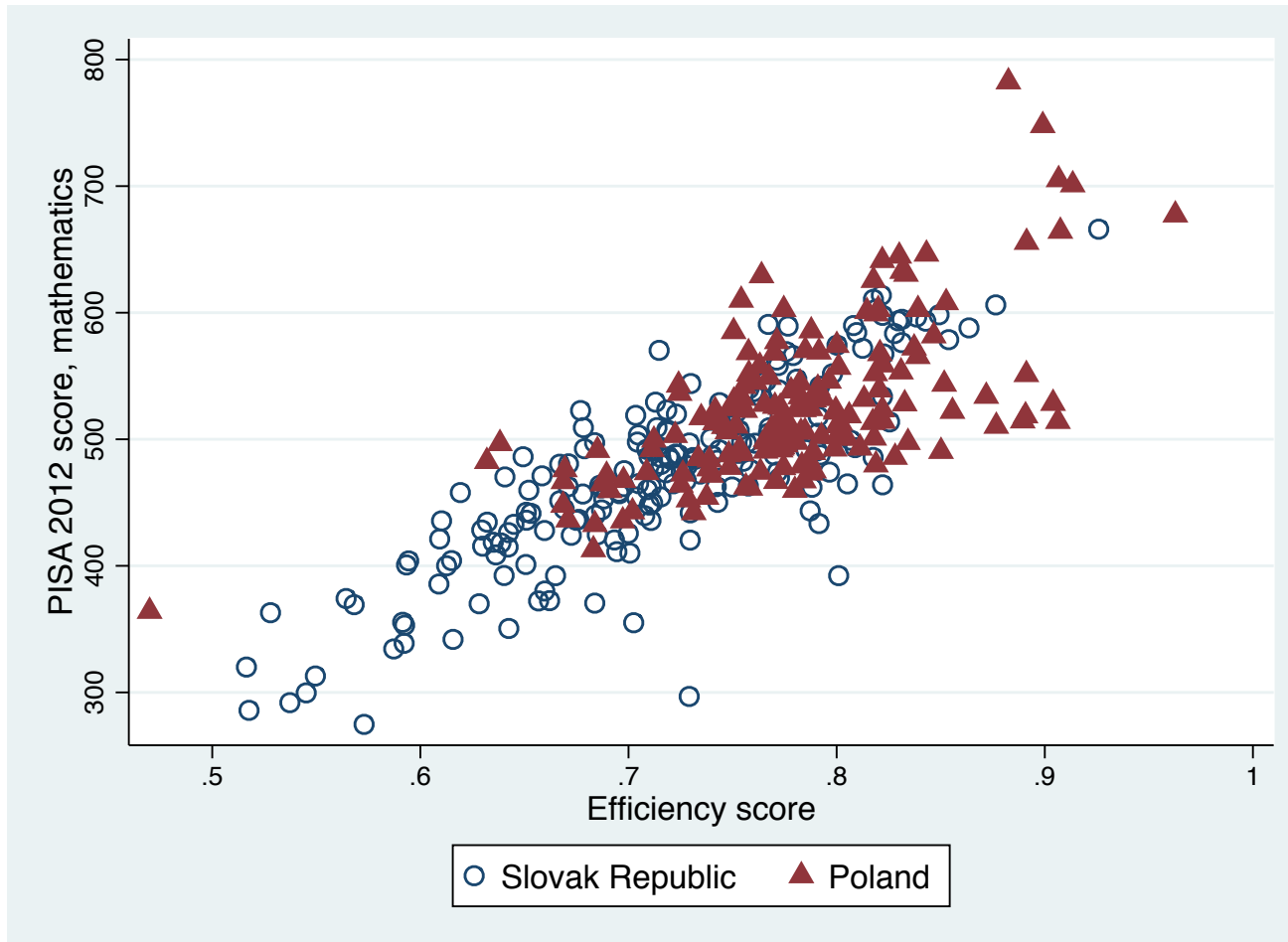




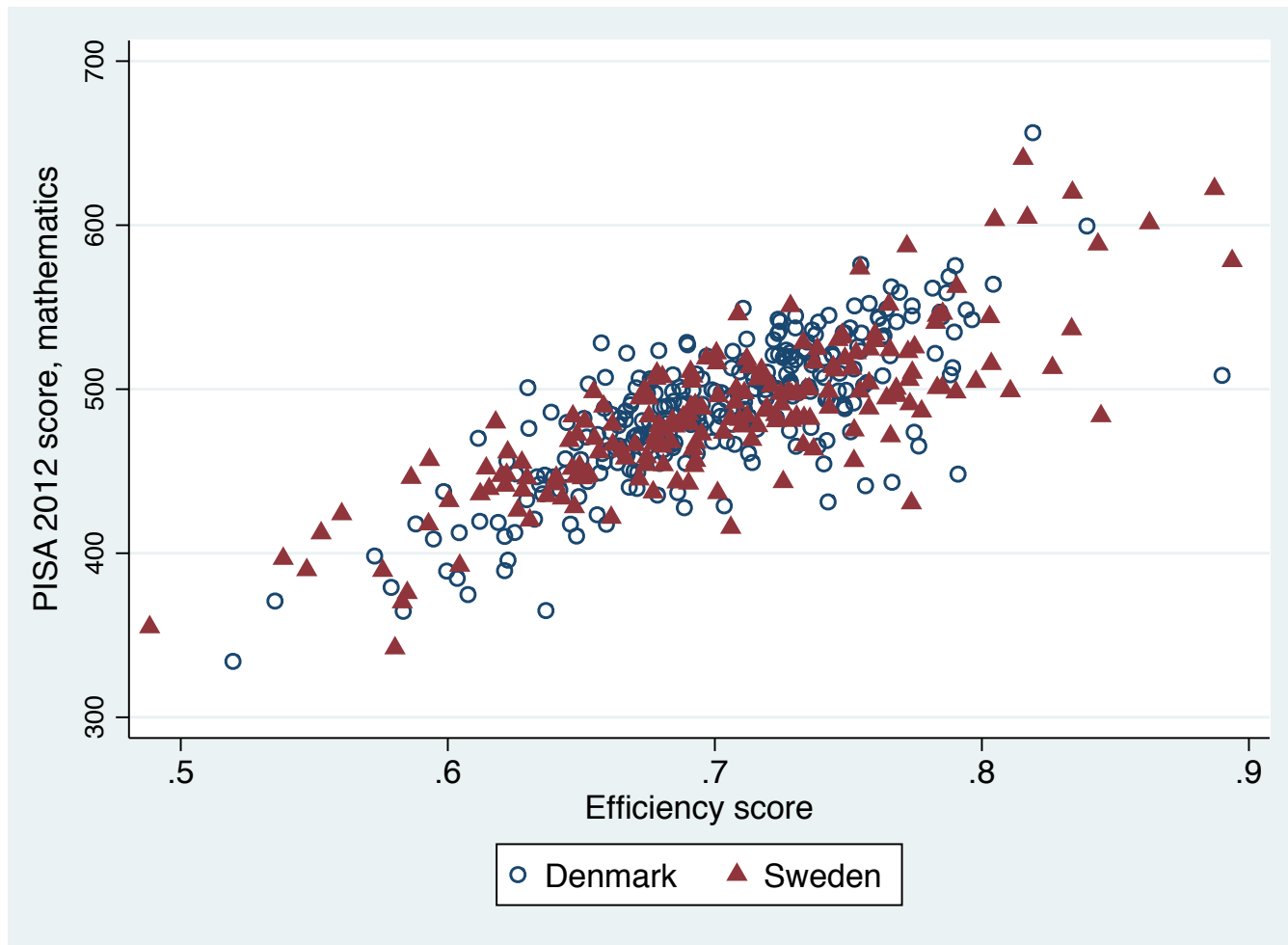
# Efficiency scores' distribution, by country



## Efficiency and performance, comparing countries (1)



## Efficiency and performance, comparing countries (2)

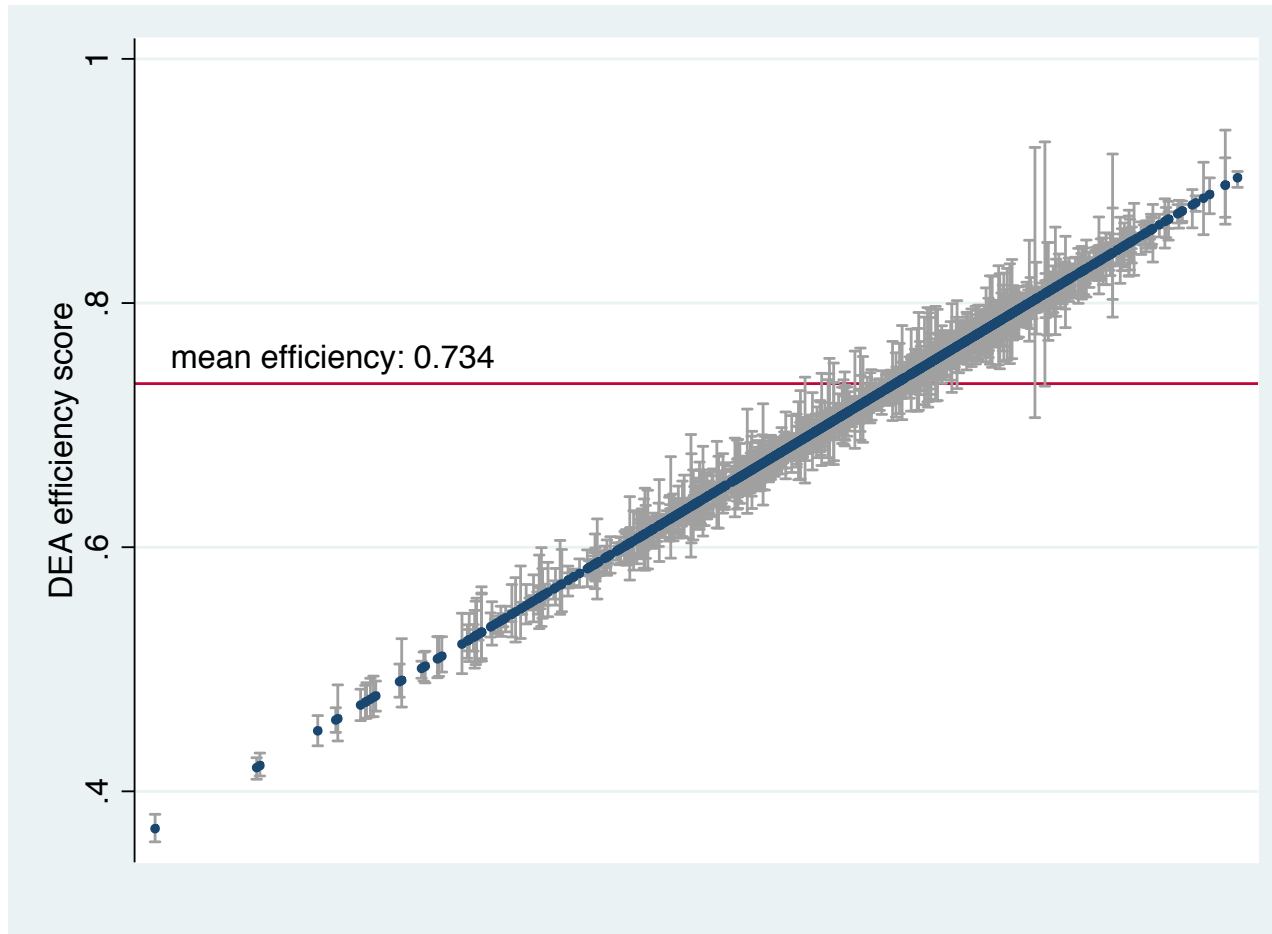


## Efficient and inefficient schools

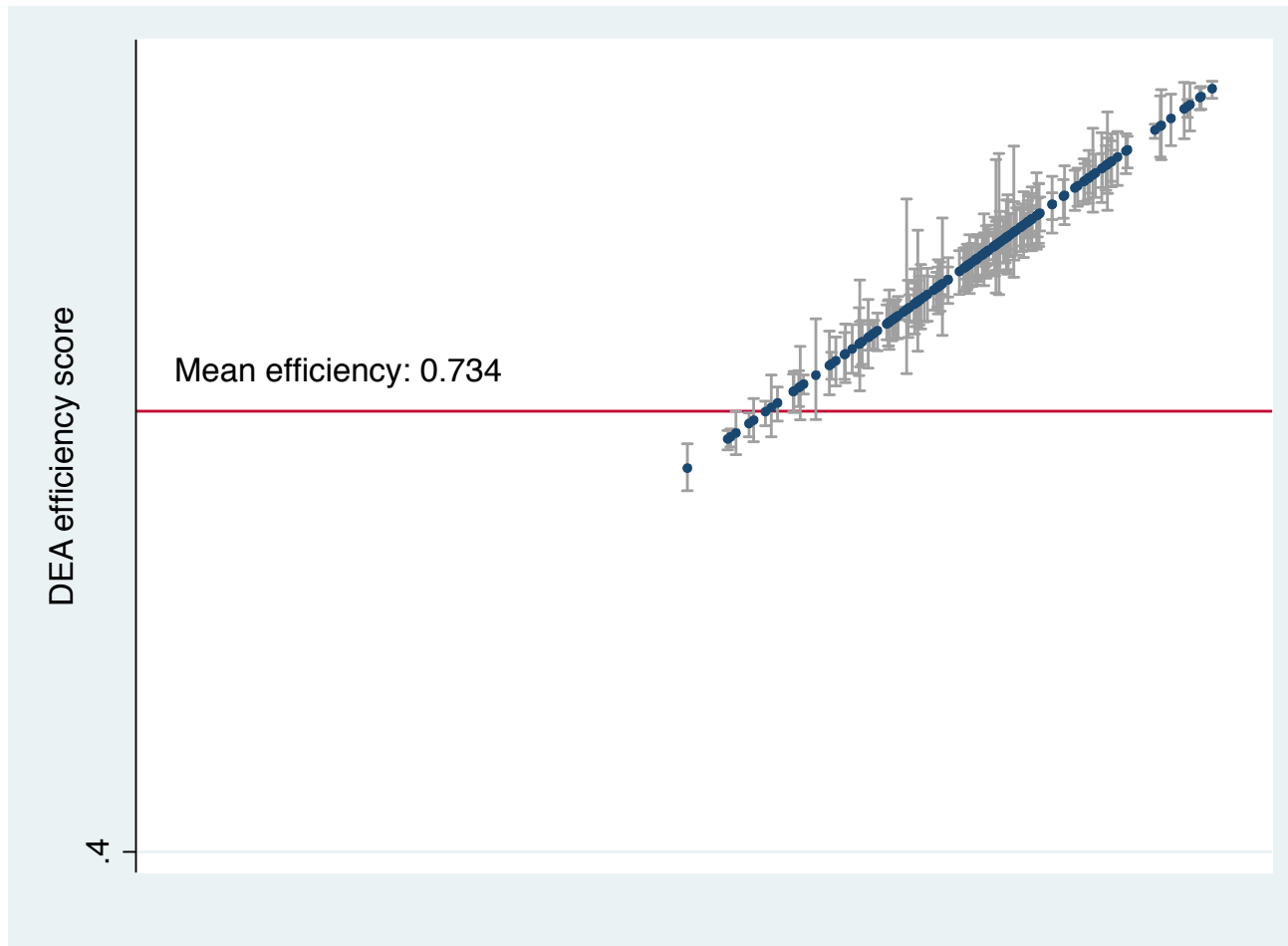
- How many schools are more/less efficient than the average, by country?  
[The CI does not cross the average value]

Selected countries	n	More efficient than avg		Less efficient than avg	
		n	%	n	%
AUS	718	369	51%	290	40%
DEU	194	110	57%	64	33%
EST	199	128	64%	51	26%
<b>IRL</b>	<b>152</b>	<b>125</b>	<b>82%</b>	<b>18</b>	<b>12%</b>
<b>ISR</b>	<b>141</b>	<b>60</b>	<b>43%</b>	<b>69</b>	<b>49%</b>
ITA	1,044	488	47%	459	44%
JPN	190	143	75%	33	17%
PRT	171	99	58%	40	23%
<b>SGP</b>	<b>163</b>	<b>155</b>	<b>95%</b>	<b>3</b>	<b>2%</b>
USA	152	73	48%	41	27%
Total	8,640	4,377	51%	3,325	38%

## Distribution of efficiency scores: ITA



# Distribution of efficiency scores: SGP



## Characteristics of very efficient schools

- Different ways of being efficient
  - Inputs and outputs of schools in the 5<sup>th</sup> percentile

Country	ESCS	StRatio	Computer_n	pvlmath	pvlread	n
AUS	0.676	0.073	1.340	<b>640.264</b>	<b>636.830</b>	18
ESP	<b>-0.436</b>	0.073	1.105	524.552	539.409	8
FRA	0.392	0.084	0.505	590.715	<b>631.255</b>	9
GBR	0.838	<b>0.064</b>	1.018	602.717	621.805	5
ITA	0.245	0.082	<b>0.378</b>	597.066	610.742	12
JPN	0.130	0.086	0.352	613.103	617.450	44
POL	<b>-0.058</b>	0.112	0.407	602.568	611.190	10
PRT	<b>-0.667</b>	0.079	0.362	527.473	540.924	5
SWE	0.759	0.069	0.831	600.166	<b>634.517</b>	2
Total	0.248	0.086	0.696	614.485	611.199	266

## Factors associated w/efficiency scores (1)

- Second-stage Tobit regression
  - Dependent variable: bias-corrected DEA score
  - Backward and forward automatic procedure over a wide set of variables
  - Robustness check: Simar & Wilson (2007) – double-bootstrap procedure [done, results qualitatively and quantitatively similar]
- Set of variables
  - **School's general characteristics** (orientation; isced2, dispersion of scores and ESCS, private, size and class size)
  - **Students' characteristics** (% females, immigrants, repeaters, students who skipped school days; hours spent for homework)
  - **Schools' practices, resources and processes**
  - Program type and country dummies



## Factors associated w/efficiency scores (2)

Positively associated w/efficiency	Negatively associated w/efficiency
<ul style="list-style-type: none"> <li>• Program's orientation: general/academic</li> <li>• % immigrant students</li> <li>• % female students</li> <li>• Hours spent for studying homework (set by teachers)</li> <li>• % certified teachers</li> <li>• Principal responsible for budget allocation</li> <li>• Principal organises meeting with teachers (instructional activity)</li> <li>• School organises volunteering</li> </ul>	<ul style="list-style-type: none"> <li>• % students below proficiency level 2</li> <li>• Private school</li> <li>• Class size avg&lt;15 students</li> <li>• Standard deviation of ESCS</li> <li>• % students who skipped 1 or more days</li> <li>• Students report bad relationships with teachers</li> <li>• Selectivity</li> <li>• Achievement data are made public</li> </ul>

## Factors associated w/efficiency scores (3)

### Heterogeneity across countries

	Statistically significant	Positively associated w/eff	Negatively associated w/eff
<b>School's general characteristics</b>			
Program's orientation: general	8	6	2
Private	14	3	11
Class size (avg) < 15 students	12	4	8
<b>Students' characteristics</b>			
<b>Standard deviation of ESCS</b>	<b>14</b>	<b>6</b>	<b>8</b>
% female students	17	17	0
<b>Hours spent for homework</b>	<b>11</b>	<b>9</b>	<b>2</b>
% students who skipped 1 or + days	17	5	12
<b>School's practices and processes</b>			
Principal responsible - budget allocation	9	8	1
Index of teachers participation/governance	7	4	3
Achievement scores publicly available	9	3	6
School organises volunteering	8	5	3
Schools practices	8	2	6
School competes for students w/2 schools or +	10	4	6

## Examples of different countries (1)

- Austria

	AUT
<b>Students' characteristics</b>	
% female students	0.05193** <i>0.018</i>
Hours spent for homework	0.01151*** <i>0.003</i>
% Repeater students	-0.17698*** <i>0.034</i>
<b>School's general characteristics</b>	
iscsd2	0.11701*** <i>0.019</i>
pv1mathsd	0.00106*** <i>0.000</i>
pv1_belowprof2	-0.06867** <i>0.021</i>
Class size, small	-0.02848 <i>0.015</i>

## Examples of different countries (2)

- Czech Republic

	CZE
<b>Students' characteristics</b>	
% immigrant students	-0.41297*** <i>0.085</i>
% female students	0.05056** <i>0.016</i>
ESCS (standard deviation)	-0.06886** <i>0.022</i>
<b>School's general characteristics</b>	
Orientation: general	0.01941* <i>0.008</i>
pv1_belowprof2	-0.13706*** <i>0.016</i>
<b>Schools' practices and processes</b>	
Principal's autonomy in budget formulation	-0.05355** <i>0.019</i>

## Examples of different countries (3)

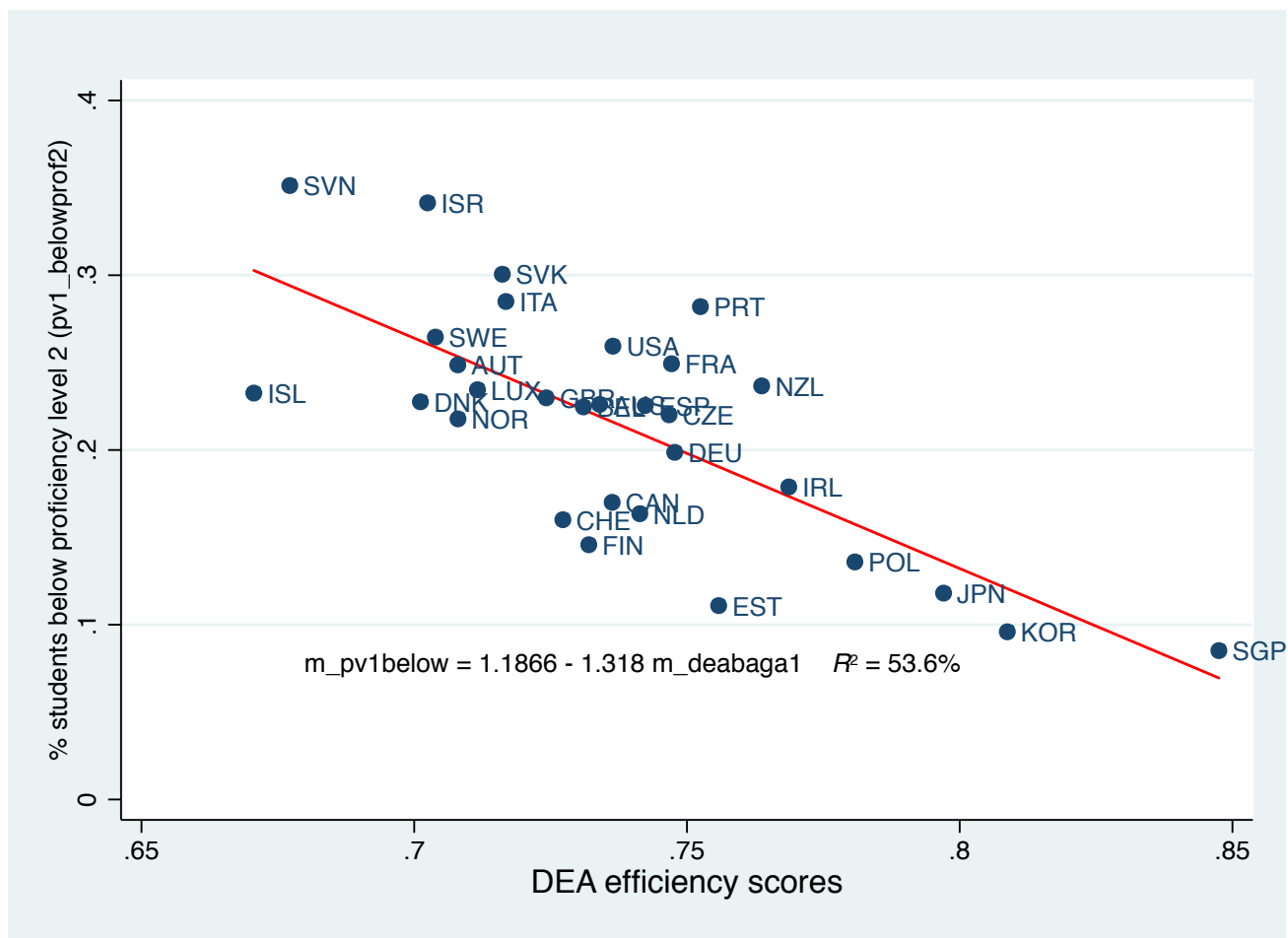
- Estonia

	EST
<b>Students' characteristics</b>	
% immigrant students	0.47389*** <i>0.122</i>
% students who skipped > one day	-0.07320** <i>0.024</i>
<b>School's general characteristics</b>	
Pv1math (standard deviation)	0.00031 <i>0.000</i>
pv1_belowprof2	-0.37525*** <i>0.031</i>
Class size, small	-0.02350** <i>0.008</i>
<b>Schools' practices and processes</b>	
Principal's autonomy in budget formulation	0.04102** <i>0.014</i>
Extracurricular activities: volunteering	0.02623*** <i>0.007</i>
Competition, >2 schools competing for same students	0.01534* <i>0.006</i>

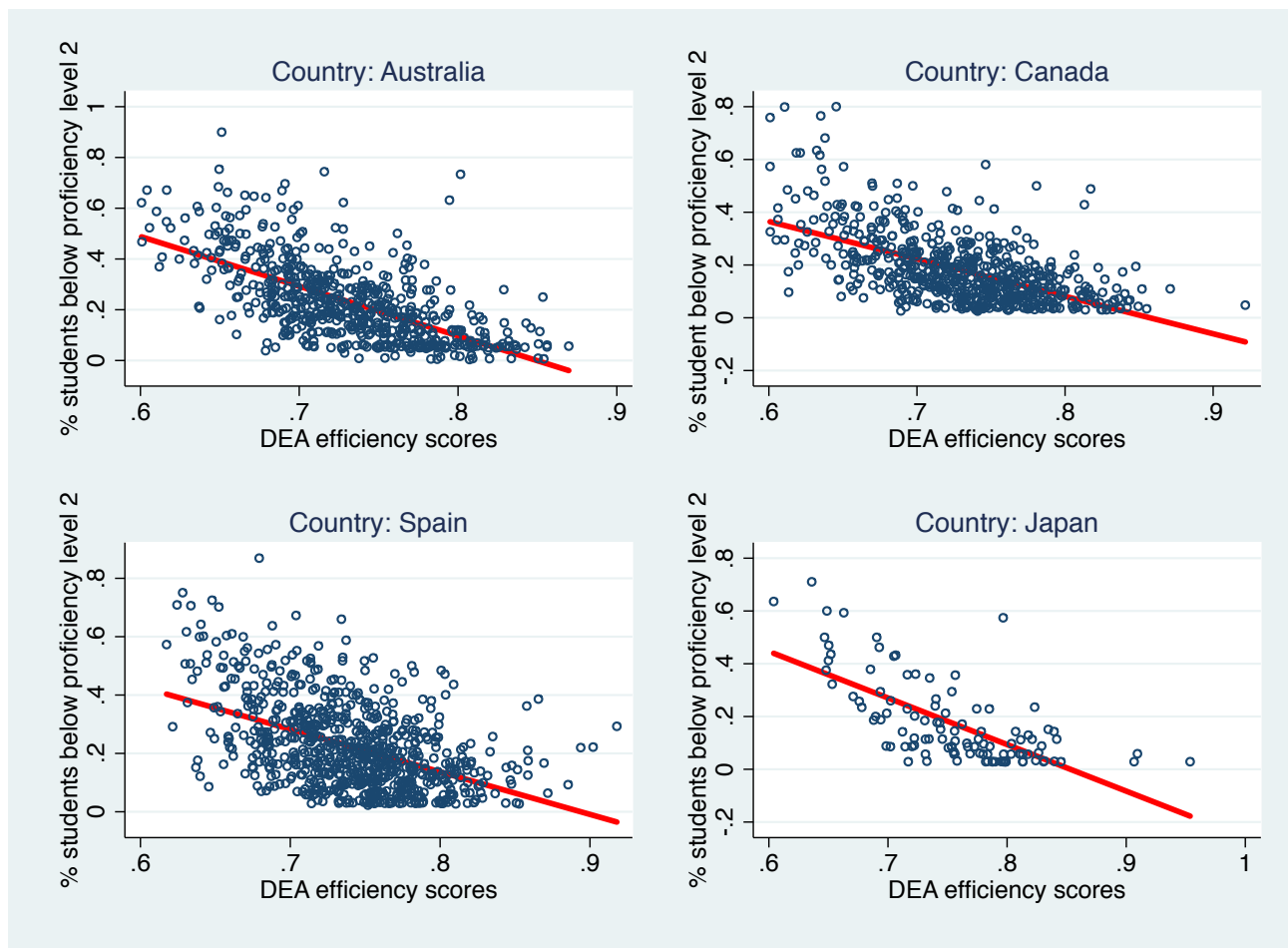
# Efficiency and equity: correlations

- Equity definition(s)
  - **Inclusion**: the proportion of students below proficiency level 2 (Schleicher, 2014)
  - **Equality**: dispersion of scores around the mean (standard deviation), similar to the concept proposed by Freeman *et al.* (2010)
- Inclusion:
  - The “automatic” relationship with performance/efficiency (the lower the proportion of low performing students, the higher the performance/efficiency, all else equal) but (i) exceptions and (ii) different possibilities (i.e. higher equality for lower means)

# Efficiency and inclusion



# Efficiency and inclusion, selected countries





## What can we learn? Policy implications

- Caution in interpreting efficiency measures → they depend on assumptions, and measure only partial phenomena
  - We are NOT looking at mechanisms for transforming inputs into outputs
- Some factors are more likely than others to be positively correlated with efficiency scores
  - (i) students' commitment (hours spent at homework, not skipping school days), (ii) schools/principals' autonomy in managing resources, (iii) extracurricular activities, ...
- Negatively associated with efficiency:
  - (i) bad school climate, (ii) high proportion of students below proficiency level 2

## Concluding remarks (1)

- Setting an international frontier for estimating schools' efficiency can be interesting if accepting the existence of comparable outputs and inputs  
→ a higher number (and types) of schools to be compared with  
[managerial implication]
  - How taking the structural differences between countries into account? The related literature about “institutional settings” (Hanushek & Woessmann, 2010)
- Within-country differences are wider than between-countries (structural) ones
  - Does it make sense comparing the efficiency of countries' educational systems *as a whole*?

## Concluding remarks (2)

- Potential extensions
  - New concepts and measures of equity → for example, proportion of resilient students
  - How the distribution of efficiency scores (within and between countries) evolved over time? → Comparing PISA 2003 and PISA 2012
  - Including some variable at country level for “explaining” structural differences in schools’ efficiency across countries
- Adding further robustness checks:
  - SFA – Stochastic Frontier Analysis (Annex)
  - Different DEA specifications (Annex)
  - Eliminating outliers (*to be done*)

# Additional materials

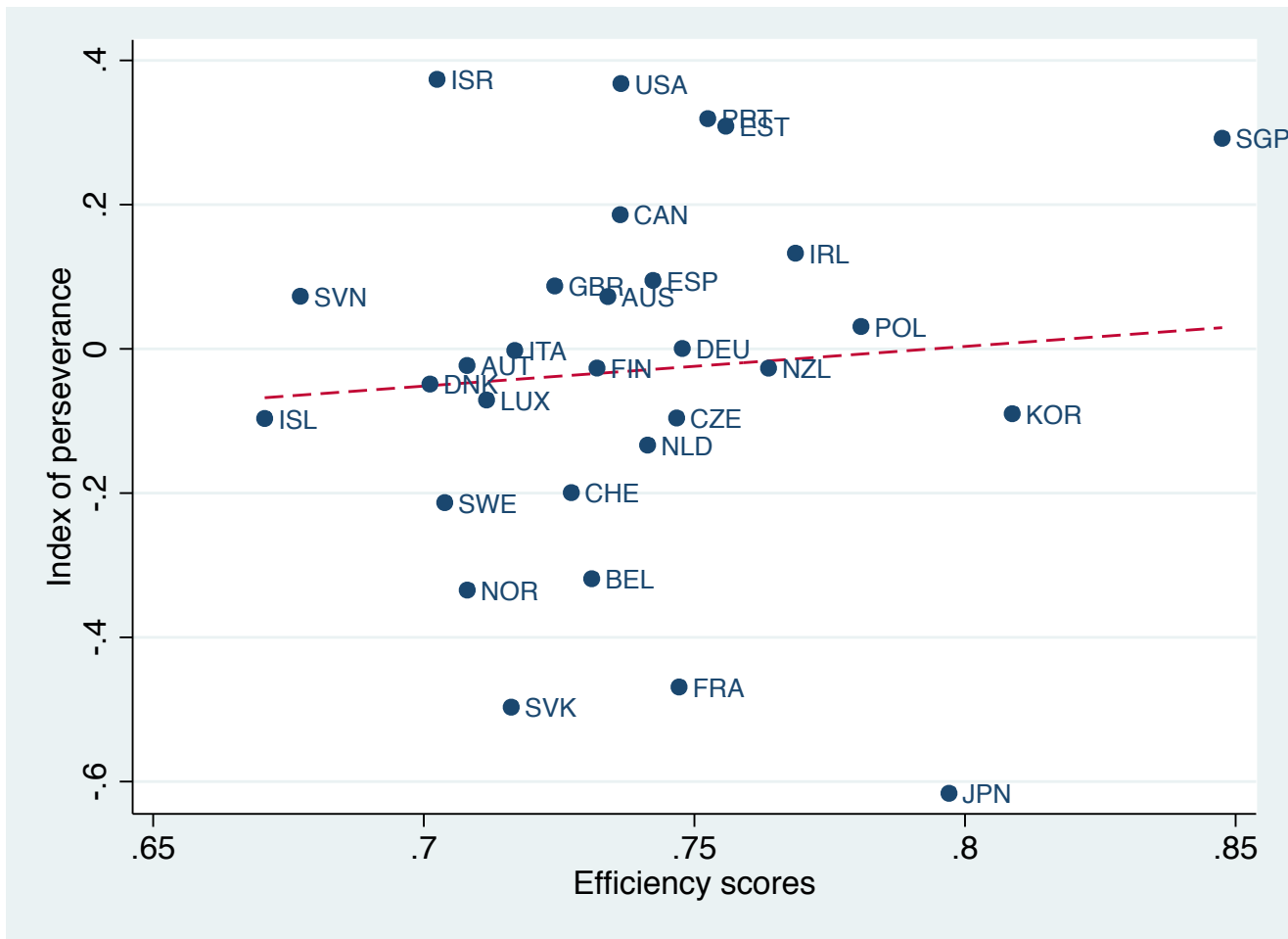
- Measures of non-cognitive skills
- Developing countries

# Measures of non-cognitive skills

- Schools do not only “produce” achievement or cognitive skills
  - OECD (2013) vol. III Students’ engagement, drive and self-beliefs
- Focus on two measures:
  - Perseverance (**persev**): constructed index based on students’ responses about their willingness to work on problems that are difficult, even when they encounter problems
  - Openness to problem solving (**openps**): constructed index based on students’ responses about their willingness to engage with problems

Both indexes: mean=0 sd=1 across OECD countries

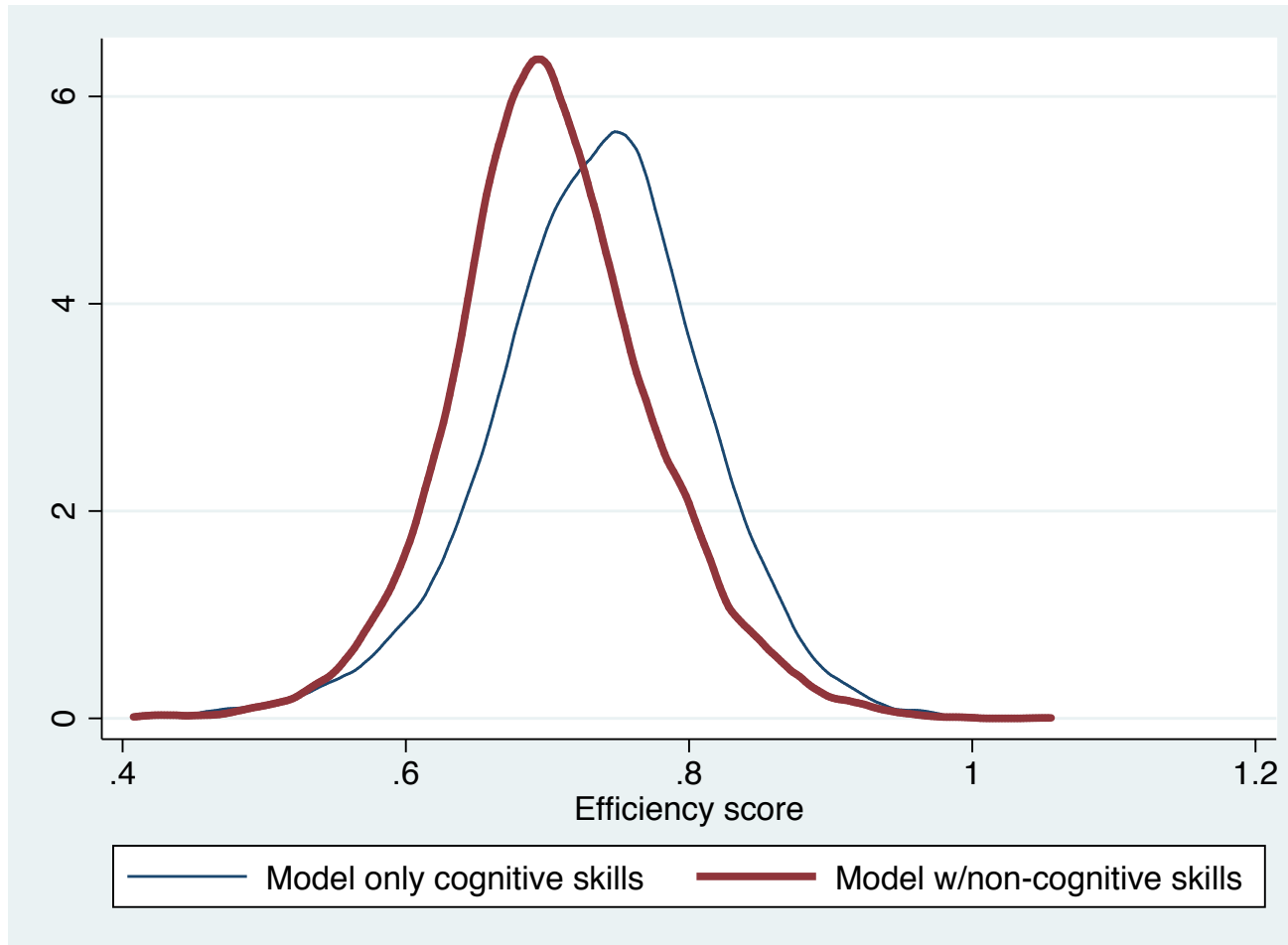
# Perseverance and efficiency, by country



## Efficiency model w/ alternative outputs

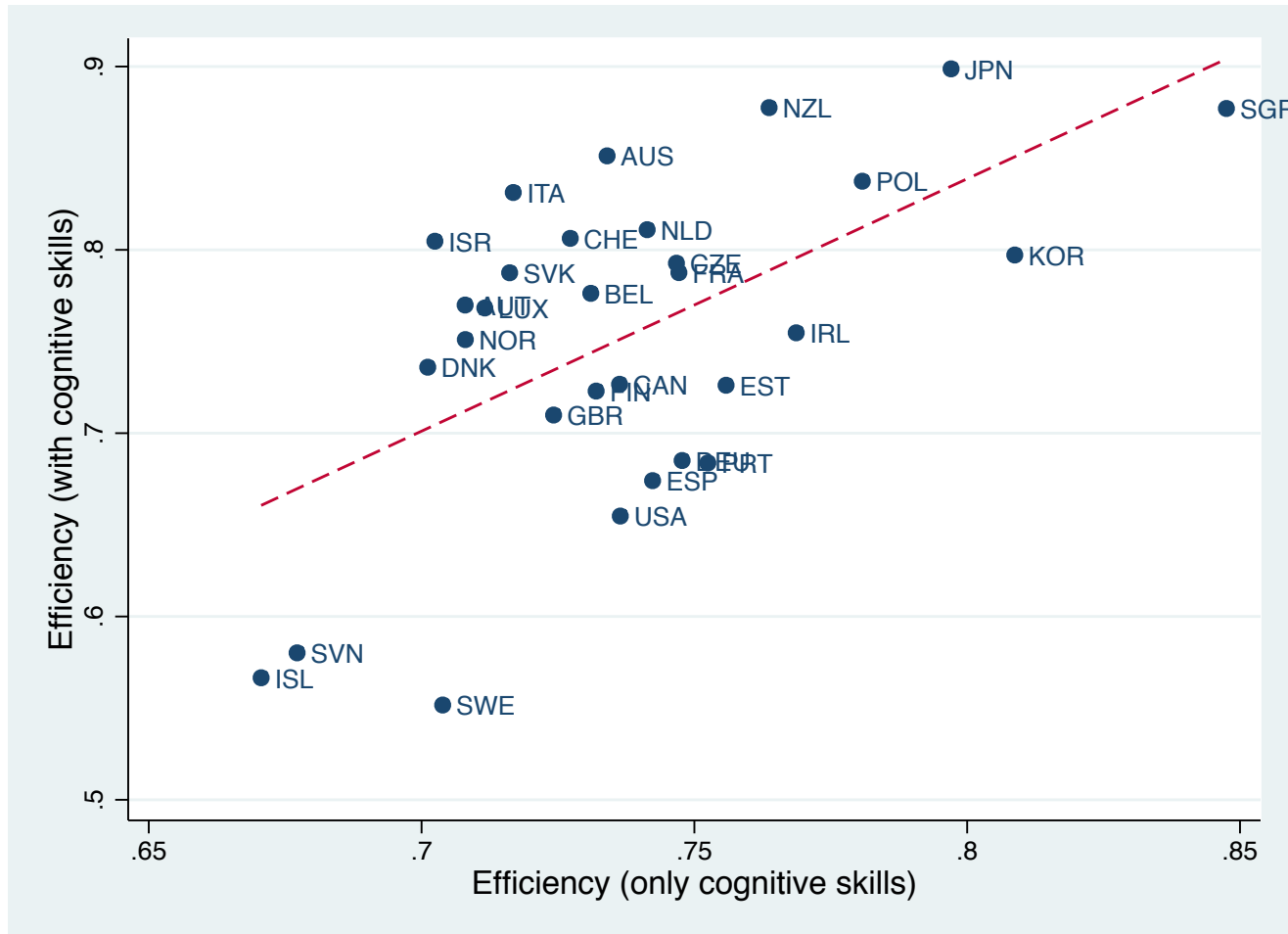
- What happens when we model schools' efficiency including *persev* as an output?
  - Inputs: as in previous model (StRatio, ESCS, Computer\_n)
  - Outputs: pv1math, *persev*
- If the results do not change substantially:
  - Achievement scores could be considered as the main drivers of the school outputs' vector

# Distribution of efficiency scores

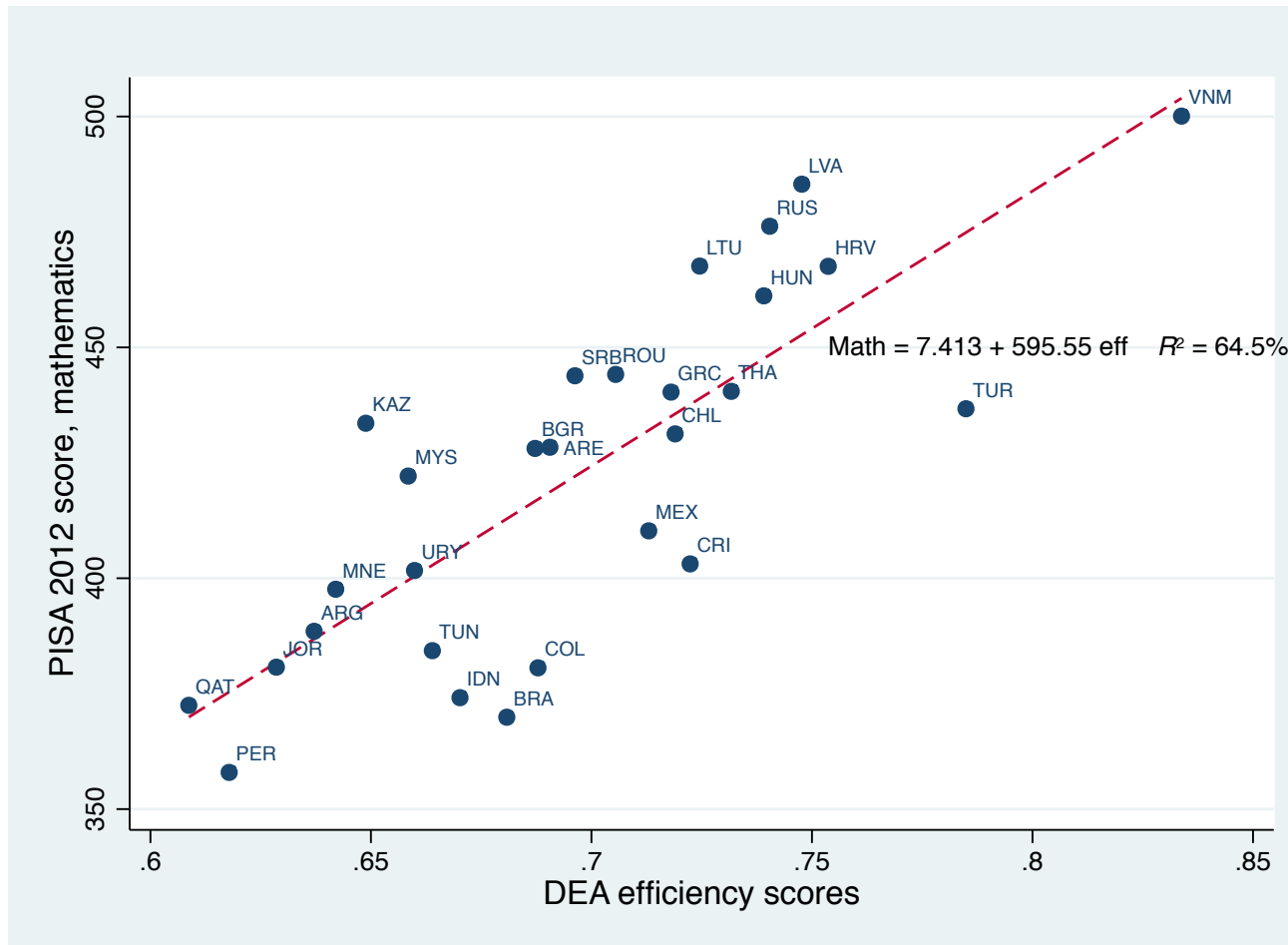




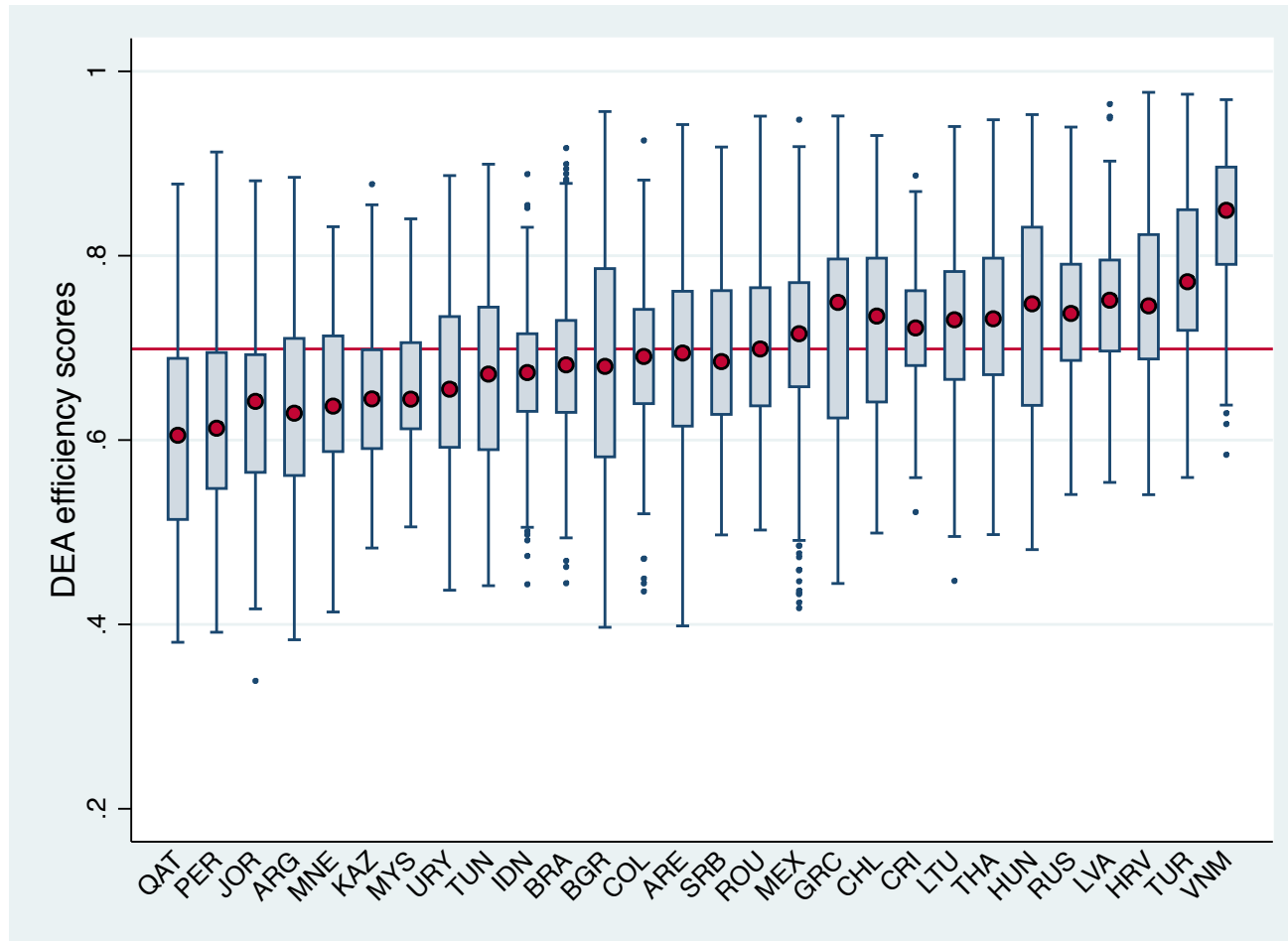
# Efficiency with and without non-cognitive



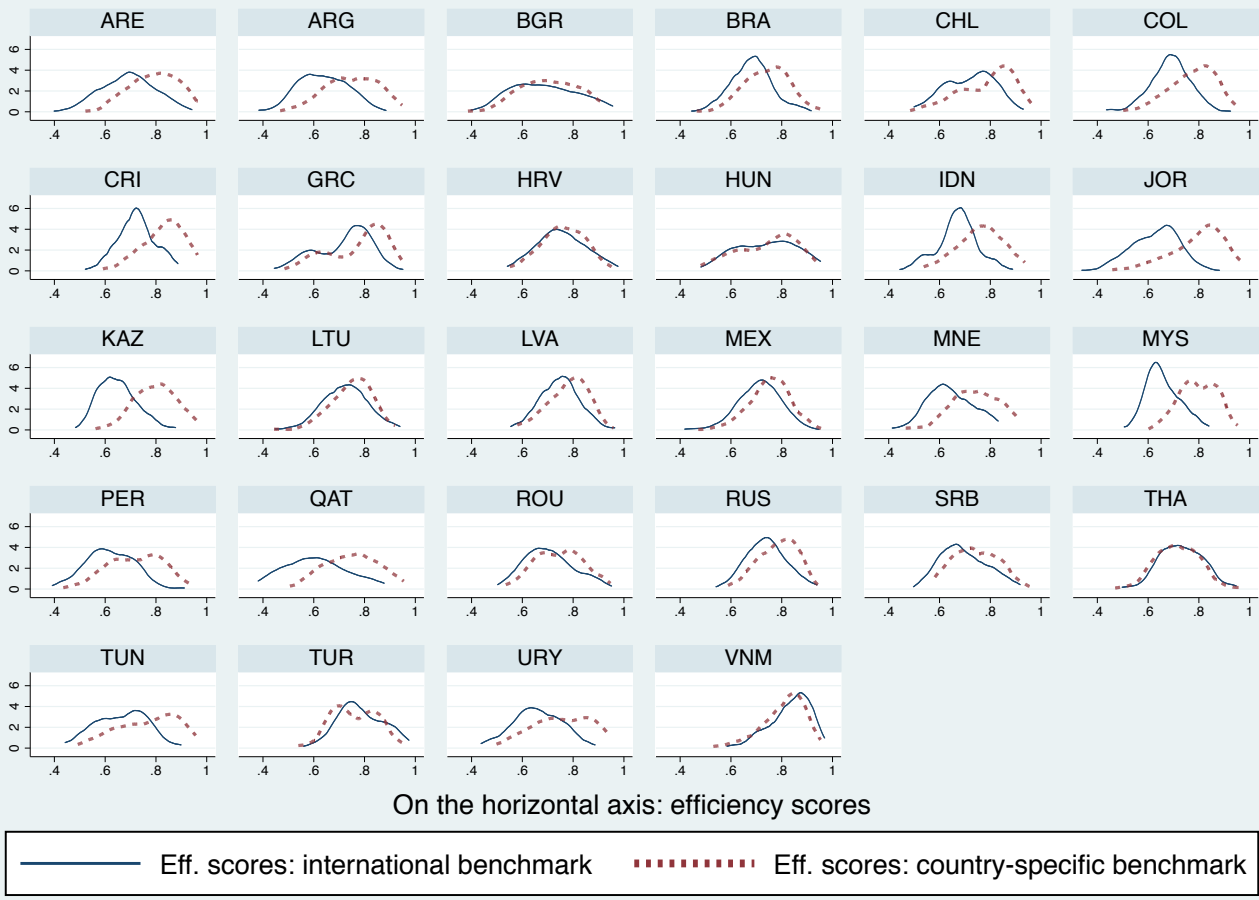
# Developing countries (1)



## Developing countries (2)

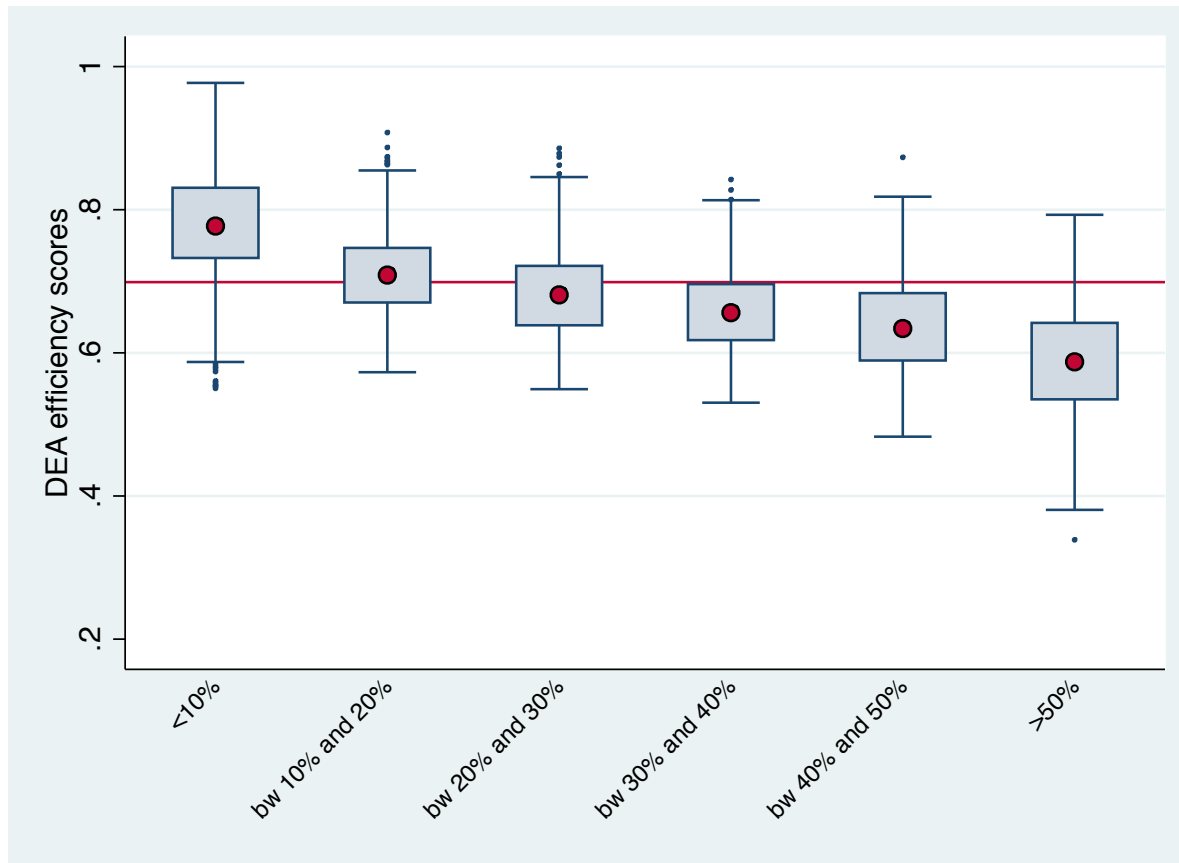


# Developing countries (3)



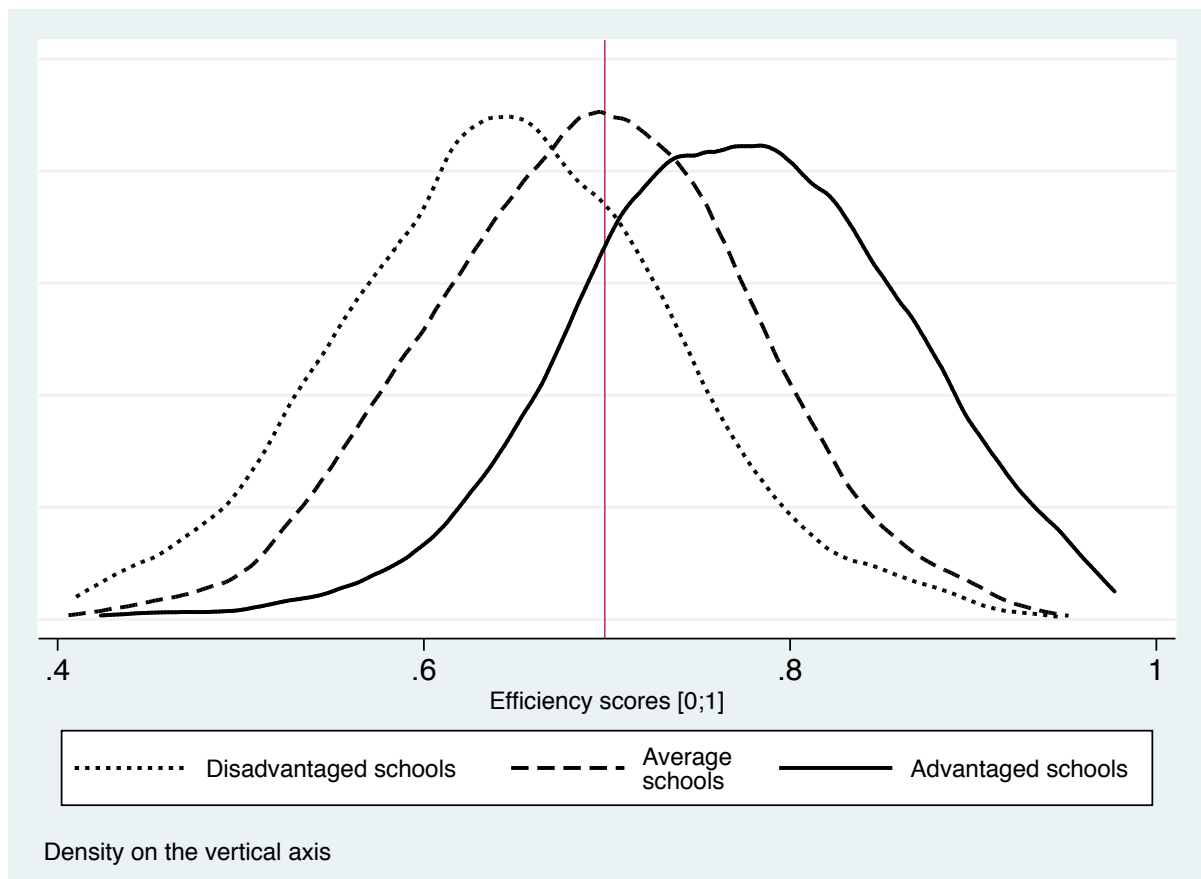
## Developing countries (4)

- % students with proficiency level <1



# Developing countries (5)

- % students with ESCS advantaged/disadvantaged



# Developing countries (6)

- Advantaged/Disadvantaged schools, by country

