

Coherencia en la enseñanza de matemáticas

MICHIGAN STATE
U N I V E R S I T Y

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Pregunta de investigación

**¿Cuál es la relación entre
currículo y logro? ó
¿Cuál es el rol de la
coherencia?**

Descripción del enfoque metodológico; análisis documental

Modelo Curricular tripartita de la IEA

*Curículo logrado:
conocimientos,
competencias y actitudes
obtenidos por los
estudiantes*

*Curículo aplicado: objetivos, estrategias y prácticas
implementadas en el salón de clase.*

*Curículo prescrito: políticas, programas y objetivos generales
del sistema educativo*

Marco TIMSS de Matemáticas – Un ejemplo

- 1 Números
- 2 Mediciones
- 3 Geometría: posiciones, visualización y formas
- 4 Geometría: simetría, congruencia y similaridad
- 5 Proporcionalidad
- 6 Funciones, relaciones y ecuaciones
- 7 Representación de datos, probabilidad y estadísticas
- 8 Análisis elemental
- 9 Validación y estructura
- 10 Otros contenidos

6,1 Patrones,
relaciones y
funciones

6,2 Ecuaciones y
fórmulas

- 6.2.1 Representación de situaciones numéricas
- 6.2.2 Solución informal de ecuaciones simples
- 6.2.3 Operaciones con expresiones
- 6.2.4 Expresiones equivalentes
- 6.2.5 Ecuaciones lineales: soluciones
- 6.2.6 Ecuaciones cuadráticas: soluciones
- 6.2.7 Ecuaciones polinomiales: soluciones
- 6.2.8 Trig identidades y ecuaciones: soluciones
- 6.2.9 Logs y ec. Exponenciales: soluciones
- 6.2.10 Solución de ecuaciones mas complejas
- 6.2.11 Otras soluciones para ecuaciones
- 6.2.12 Inequidades: soluciones gráficas
- 6.2.13 Sistemas de ecuaciones: soluciones
- 6.2.14 Sistemas de inequidades: soluc & gráficas
- 6.2.15 Sustituir/arreglar fórmulas
- 6.2.16 Ecuación general de segundo grado

Dos “mapas de seguimiento de tópicos”



Ejemplos del Indice IGP

Código	Descripción	Indice IGP
1111	Números enteros: significado	1,8
1122	Fracciones decimales	4,6
1141	Aritmética binaria &/o base de otros números	6,6
1143	Números complejos y sus propiedades	10,7
141	Transformaciones geométricas	7,1
151	Conceptos de proporcionalidad	6,4
161	Patrones, relaciones & funciones	9,0
162	Ecuaciones & fórmulas	7,0
171	Representación de datos & análisis	7,4
172	Incertidumbre y probabilidad	9,7
181	Elementary Analysis: Procesos infinitos	11,5

Constructos de contenido instruccional

❖ Coherencia curricular

- ▣ Estructura curricular

❖ Foco curricular

- ▣ Tiempo de exposición (OTL)

❖ Rigor curricular

- ▣ Nivel de complejidad cognitiva

Definición de coherencia

Los contenidos estándar, en el agregado, son **coherentes** si están **articulados en el tiempo**, como una secuencia de tópicos y desempeños **consistentes con la lógica de contenido de la disciplina de la cual se deriva el tema** de estudio, y de su naturaleza jerárquica. Esto **no implica una única secuencia coherente**; sólo que la secuencia refleje la estructura inherente de la disciplina.

Definición de coherencia

En otras palabras, hay coherencia si la secuencia de tópicos a través de los grados escolares es consistente con la estructura lógica de las matemáticas. Si los pre-requisitos se cubren antes de los tópicos avanzados.

Matemáticas son acumulativas

- Bien hechos, los tópicos en cada año dependen de los tópicos cubiertos en años anteriores.
- Cuando no se tiene en cuenta su naturaleza acumulativa, el estudio de las matemáticas degenera en una lista de cosas por hacer, sin significado, y de memorización de hechos desconectados entre sí, lo que afecta especialmente a los estudiantes más débiles.

*James Milgram, Professor of Mathematics, Stanford University
MSU Education Policy Forum, Washington, DC, June, 2003*

Currículo de matemáticas de países con mayor logro

Topic	Grade											
	1	2	3	4	5	6	7	8	9	10	11	12
Whole Number: Meaning	●	●										
Whole Number: Operations	●	●	●	●	●	●						
Measurement Units	●	●	●	●	●	●	●					
Common Fractions			●	●	●	●	●					
Equations & Formulas			●	●	●	●	●	●	●	●	●	●
Data Representation & Analysis			●	●	●	●	●					
2-D Geometry: Basics			●	●	●	●	●	●				
2-D Geometry: Polygons & Circles			●	●	●	●	●	●	●	●		
Measurement: Perimeter, Area & Volume			●	●	●	●	●	●	●			
Rounding & Significant Figures			●	●	●	●						
Estimating Computations			●	●	●	●						
Whole Numbers: Properties of Operations			●	●	●	●						
Estimating Quantity & Size			●	●	●							
Decimal Fractions			●	●	●	●	●					
Relation of Common & Decimal Fractions			●	●	●	●	●					
Properties of Common & Decimal Fractions			●	●	●	●	●					
Percentages			●	●	●	●	●					
Proportionality Concepts			●	●	●	●	●	●	●	●		
Proportionality Problems			●	●	●	●	●	●	●	●		
2-D Geometry: Coordinate Geometry			●	●	●	●	●	●	●	●		
Geometry: Transformations			●	●	●	●	●	●	●			
Negative Numbers, Integers, & Their Properties			●	●	●	●	●					
Number Theory			●	●	●	●	●	●				
Exponents, Roots & Radicals			●	●	●	●	●	●	●			
Exponents & Orders of Magnitude			●	●	●	●	●	●				
Measurement: Estimation & Errors			●	●	●							
Constructions Using Straightedge & Compass			●	●	●	●	●	●				
3-D Geometry			●	●	●	●	●	●	●	●	●	●
Geometry: Congruence & Similarity			●	●	●	●	●	●				
Rational Numbers & Their Properties			●	●	●	●	●	●				
Patterns, Relations & Functions			●	●	●	●	●	●	●	●	●	●
Proportionality: Slope & Trigonometry			●	●	●	●	●	●				
Real Numbers, Their Subsets & Properties			●	●	●	●	●	●				
Validation & Justification			●	●	●	●	●	●	●	●	●	●
Structuring & Abstracting			●	●	●	●	●	●				
Uncertainty & Probability			●	●	●	●	●	●				
Complex Numbers & Their Properties			●	●	●	●	●	●				
Infinite Processes			●	●	●	●	●	●	●	●	●	●
Change			●	●	●	●	●	●	●	●	●	●
Vectors			●	●	●	●	●	●	●	●	●	●
Systematic Counting			●	●	●	●	●	●	●	●	●	●

● Intended by 4, 5, or 6 of the top achieving countries

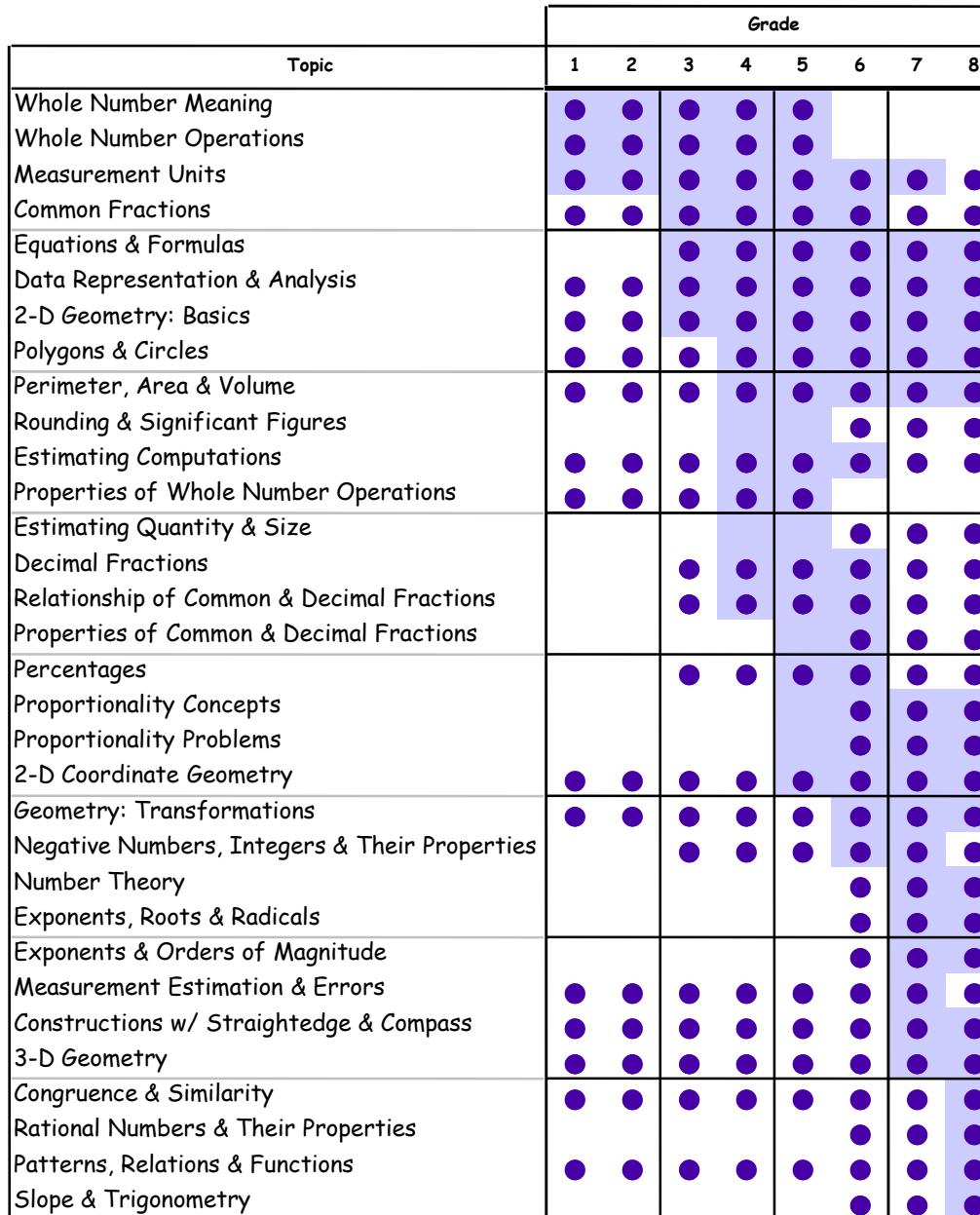
Matemáticas programadas para cada grado, en países de mayor logro

Topic	Grade							
	1	2	3	4	5	6	7	8
Whole Number: Meaning	●	●		●	●			
Whole Number: Operations	●	●	●	●	●			
Measurement Units	●	●	●	●	●	●	●	
Common Fractions		●	●	●	●	●	●	
Equations & Formulas			●	●	●	●	●	●
Data Representation & Analysis			●	●	●	●	●	
2-D Geometry: Basics			●	●	●	●	●	
2-D Geometry: Polygons & Circles				●	●	●	●	
Measurement: Perimeter, Area & Volume				●	●	●	●	
Rounding & Significant Figures				●	●	●	●	
Estimating Computations				●	●	●	●	
Whole Numbers: Properties of Operations				●	●	●	●	
Estimating Quantity & Size				●	●	●	●	
Decimal Fractions				●	●	●	●	
Relation of Common & Decimal Fractions				●	●	●	●	
Properties of Common & Decimal Fractions				●	●	●	●	
Percentages					●	●	●	
Proportionality Concepts					●	●	●	
Proportionality Problems					●	●	●	
2-D Geometry: Coordinate Geometry					●	●	●	
Geometry: Transformations						●	●	
Negative Numbers, Integers, & Their Properties						●	●	
Number Theory						●	●	
Exponents, Roots & Radicals						●	●	
Exponents & Orders of Magnitude							●	
Measurement: Estimation & Errors							●	
Constructions Using Straightedge & Compass							●	
3-D Geometry							●	
Geometry: Congruence & Similarity								●
Rational Numbers & Their Properties								●
Patterns, Relations & Functions								●
Proportionality: Slope & Trigonometry								●

Intended by at least two-thirds of the top-achieving countries



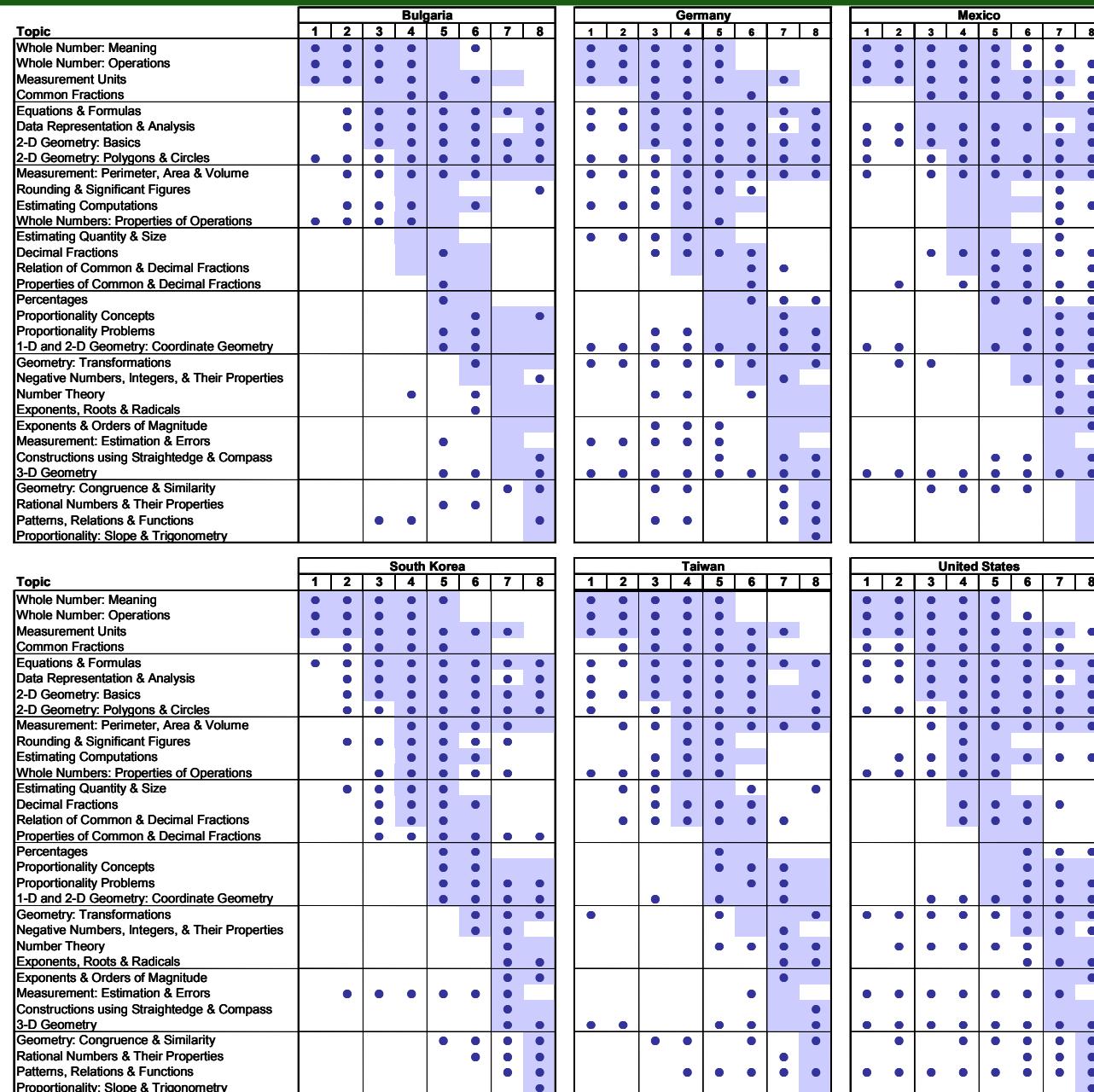
2000 NCTM Estándares de Matemáticas



Top Achieving Countries' Profile
Topic Intended



Matemáticas programadas para cada grado, en 6 países



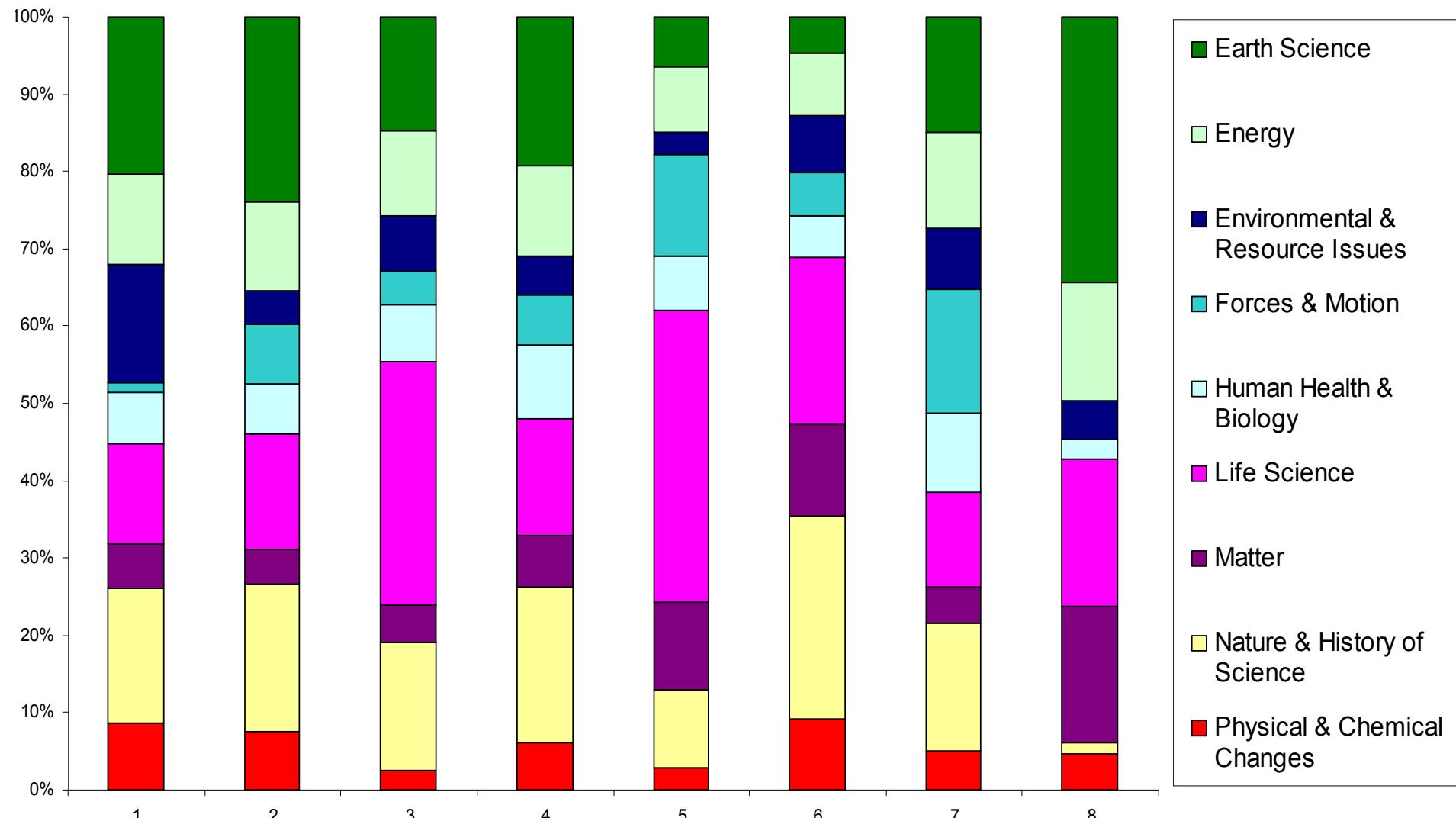
Evaluación sensible al currículo

Midiendo el currículo aplicado

- **Temas cubiertos en clase**
- **Los maestros indican el número de clases en las que cubren un tema**
- **Lista de temas proviene de un marco general**
- **El nivel de cubrimiento de un tema por parte del maestro puede ser evaluado en relación con el desempeño de los estudiantes y con los temas del marco general**
- **La relación puede ser examinada a nivel del salón ó del colegio**

Ejemplo de Currículo Aplicado

Tiempo promedio de enseñanza de 9 áreas de ciencias



Diseño de evaluaciones sensibles al currículo

- Sirven para descubrir lo que los estudiantes saben en cada grado (3º - 12º) en múltiples áreas;
- Evaluaciones apropiadas para 3 grados;
- Cada evaluación tiene diferentes formatos creados utilizando un muestreo matricial de items;
- Diseñado para brindar un amplio cubrimiento de las áreas;
- Los formatos se distribuyen al azar al interior de cada salón de clase.

Por qué es importante la evaluación sensible al currículo

Desempeño en tópicos específicos en matemáticas 1995 TIMSS

Whole Numbers	Common Fractions	Decimal Fractions & Percentages	Relationships of Fractions	Estimations of Quantity/Size	Rounding	Estimating Computations	Measurement Units	Perimeter, Area, Volume	Measurement Estimations & Errors
Singapore	80.4	Singapore	82.4	Singapore	85.1	Japan	77.9	Singapore	84.5
Japan	72.0	Japan	72.2	Korea	77.6	Singapore	77.3	Czech Republic	82.9
Switzerland	70.2	Korea	69.9	Hong Kong	71.1	England	72.2	Japan	81.0
Belgium (Fl)	68.6	Hong Kong	69.4	Japan	69.8	Hong Kong	71.8	Hong Kong	80.8
Austria	68.4	Belgium (Fl)	68.7	Slovak Republic	69.1	Belgium (Fl)	71.3	Korea	79.5
Korea	67.6	Switzerland	62.4	Hungary	68.7	Switzerland	70.0	Austria	78.9
Czech Republic	67.4	Ireland	61.7	Korea	68.4	Czech Republic	71.7	Czech Republic	78.2
Hong Kong	65.4	Austria	60.4	Austria	66.6	France	67.2	Slovak Republic	77.7
Slovak Republic	64.6	Belgium (Fr)	59.8	Russian Federation	65.9	Belgium (Fr)	65.8	Belgium (Fl)	77.7
France	64.5	Slovenia	59.7	Belgium (Fr)	65.9	Korea	70.7	Sweden	76.1
Slovenia	63.4	Czech Republic	59.6	Belgium (Fr)	64.6	Austria	69.9	USA	75.2
Russian Federation	62.7	Netherlands	58.9	Czech Republic	64.9	Australia	69.3	Bulgaria	75.2
Bulgaria	62.5	Slovak Republic	58.6	Belgium (Fl)	64.6	Sweden	78.5	Russian Federation	74.5
Ireland	62.2	Switzerland	57.8	Ireland	64.3	Hungary	69.3	Denmark	74.5
Spain	60.8	France	57.8	Slovak Republic	63.0	Sweden	69.3	France	74.5
Hungary	60.6	Hungary	57.7	Canada	61.0	Slovak Republic	69.1	Netherlands	73.0
Sweden	58.9	Israel	57.4	Canada	61.0	Germany	62.6	Belgium (Fr)	72.9
Canada	57.9	Belgium (Fr)	58.6	Canada	61.0	Netherlands	62.5	Hungary	72.7
Israel	59.0	Thailand	54.2	Canada	61.0	Slovenia	62.4	Australia	72.5
Thailand	56.0	Bulgaria	54.2	Canada	61.0	Germany	69.0	Japan	72.5
International	55.7	Bulgaria	54.2	Germany	57.2	Thailand	59.6	Thailand	72.5
Germany	55.4	Sweden	53.1	Germany	57.2	Slovenia	65.5	New Zealand	72.5
Latvia	55.4	International	52.3	Thailand	59.6	Thailand	75.4	Denmark	72.5
Belgium (Fr)	55.4	Cyprus	51.9	Thailand	58.0	Thailand	75.4	Thailand	72.5
Australia	55.0	International	55.5	Netherlands	57.8	Thailand	75.4	Thailand	72.5
Lithuania	53.8	Germany	51.7	Australia	61.0	Thailand	75.4	Thailand	72.5
Netherlands	53.5	New Zealand	51.5	Hungary	60.7	Thailand	75.4	Thailand	72.5
Norway	53.4	Norway	51.2	International	57.0	Thailand	75.4	Thailand	72.5
Greece	52.7	Australia	51.2	Bulgaria	62.4	Thailand	75.4	Thailand	72.5
USA	52.3	USA	49.3	International	70.9	Thailand	75.4	Thailand	72.5
Romania	52.3	Scotland	49.3	International	70.9	Thailand	75.4	Thailand	72.5
Denmark	51.0	Iceland	49.2	International	61.1	Thailand	75.4	Thailand	72.5
Portugal	49.0	Denmark	49.0	International	61.1	Thailand	75.4	Thailand	72.5
New Zealand	48.6	Latvia	47.3	International	61.1	Thailand	75.4	Thailand	72.5
Iceland	48.4	Greece	47.0	International	61.1	Thailand	75.4	Thailand	72.5
Scotland	47.9	Iceland	44.4	International	61.1	Thailand	75.4	Thailand	72.5
England	46.8	Lithuania	39.1	International	61.1	Thailand	75.4	Thailand	72.5
Cyprus	45.8	Iran	37.9	International	61.1	Thailand	75.4	Thailand	72.5
Iran	43.4	Portugal	34.8	International	61.1	Thailand	75.4	Thailand	72.5
Philippines	38.0	Philippines	30.0	International	61.1	Thailand	75.4	Thailand	72.5
Colombia	34.2	Colombia	27.3	International	61.1	Thailand	75.4	Thailand	72.5
Kuwait	26.4	Kuwait	25.2	International	61.1	Thailand	75.4	Thailand	72.5
South Africa	26.0	South Africa	20.2	International	61.1	Thailand	75.4	Thailand	72.5

Promedio Internacional

Promedio Bélgica (Fr)

Desempeño en tópicos específicos en matemáticas 1995 TIMSS

Whole Numbers	Common Fractions	Decimal Fractions & Percentages	Relationships of Fractions	Estimations of Quantity/Size	Rounding	Estimating Computations	Measurement Units	Perimeter, Area, Volume	Measurement Estimations & Errors
Singapore 80.4	Singapore 82.4	Singapore 77.9	Singapore 85.1	Japan 77.9	Czech Republic 86.9	Singapore 75.8	Singapore 77.9	Singapore 84.5	Czech Republic 82.9
Japan 72.0	Japan 72.2	Czech Republic 72.5	Korea 69.9	Singapore 77.6	Singapore 86.6	Czech Republic 69.8	Japan 74.8	Japan 72.6	Singapore 81.0
Switzerland 70.2	Korea 69.9	Hong Kong 71.1	Japan 69.8	Japan 75.3	Canada 84.7	Japan 69.0	Czech Republic 73.2	Hong Kong 63.9	Sweden 80.8
Belgium (Fl) 68.6	Hong Kong 69.4	Japan 69.8	Hong Kong 74.1	Hong Kong 71.8	Korea 83.8	Korea 66.7	Slovenia 72.0	Korea 61.8	Korea 79.5
Austria 68.4	Belgium (Fl) 68.7	Slovak Republic 69.1	Belgium (Fl) 71.3	Switzerland 71.8	Iceland 83.1	Belgium (Fl) 64.1	Slovak Republic 71.9	Austria 50.4	Belgium (Fl) 78.9
Korea 67.6	Switzerland 62.4	Hungary 68.7	Switzerland 70.0	Czech Republic 71.7	Slovak Republic 82.4	Switzerland 71.8	Belgium (Fl) 71.8	Czech Republic 48.9	Hungary 78.2
Czech Republic 67.4	Ireland 61.7	Korea 68.4	France 67.2	Netherlands 71.2	Canada 61.3	Slovak Republic 60.5	Sweden 69.5	Switzerland 46.6	Austria 77.7
Hong Kong 65.4	Austria 60.4	Austria 66.6	Austria 66.8	Belgium (Fl) 70.7	Belgium (Fl) 81.0	Australia 59.1	France 69.0	Slovenia 45.8	Netherlands 76.1
Slovak Republic 64.6	Belgium (Fr) 59.8	Russian Federation 65.9	Belgium (Fr) 65.8	Korea 70.7	Hungary 79.8	Bulgaria 68.1	Belgium (Fl) 45.6	France 75.2	Slovak Republic 75.2
France 64.5	Slovenia 59.7	France 64.9	Canada 65.1	Austria 69.9	USA 79.2	Ireland 60.0	Bulgaria 45.2	Slovak Republic 75.2	Australia 74.5
Slovenia 63.4	Czech Republic 59.6	Belgium (Fl) 64.6	Austria 69.9	Australia 69.3	Netherlands 78.5	Australia 59.1	Belgium (Fr) 68.1	France 75.2	Belgium (Fl) 78.9
Russian Federation 62.7	Netherlands 58.9	Slovenia 62.9	Ireland 64.3	Hungary 69.3	Sweden 78.5	Bulgaria 58.9	Bulgaria 68.1	Denmark 73.0	Denmark 73.0
Bulgaria 62.5	Slovak Republic 58.6	Switzerland 61.9	Slovak Republic 63.0	Sweden 69.3	Australia 77.5	Netherlands 58.7	Hong Kong 57.8	Netherlands 44.0	Denmark 73.0
Ireland 62.2	France 57.8	Canada 61.0	Germany 62.6	Slovak Republic 69.1	Switzerland 77.4	Hong Kong 57.8	New Zealand 57.6	Belgium (Fr) 43.0	Germany 72.9
Spain 60.8	Hungary 57.7	Sweden 59.2	Netherlands 62.5	France 69.0	Ireland 76.5	New Zealand 57.6	Hungary 67.5	Hong Kong 72.7	Hong Kong 72.7
Hungary 60.6	Israel 57.4	Belgium (Fr) 58.6	Slovenia 62.4	Germany 69.0	Austria 75.9	Hungary 57.3	Netherlands 66.8	Hungary 42.9	Australia 72.5
Sweden 58.9	Canada 56.2	Thailand 58.0	Sweden 62.2	Canada 67.8	Thailand 75.4	Norway 57.0	Norway 66.4	Japan 72.5	Japan 72.5
Canada 57.9	Russian Federation 55.8	Netherlands 57.8	Australia 61.0	Scotland 68.8	France 74.7	USA 55.7	Russian Federation 65.9	Canada 40.4	Slovenia 72.5
Israel 59.0	Australia 55.4	Bulgaria 57.8	Hungary 60.7	Scotland 66.6	Slovenia 74.7	Iceland 54.7	Denmark 65.4	England 40.0	England 71.8
Thailand 56.0	Thailand 54.2	Ireland 57.3	Bulgaria 59.9	Belgium (Fr) 65.8	New Zealand 74.4	England 54.4	Hong Kong 65.2	Ireland 39.4	New Zealand 70.6
International 55.7	Bulgaria 54.2	Germany 57.2	Thailand 59.6	Slovenia 65.5	Hong Kong 74.2	Slovenia 52.6	Australia 65.0	Sweden 39.3	Scotland 69.9
Germany 55.4	International 52.3	Israel 56.3	Norway 59.6	New Zealand 65.3	Russian Federation 73.5	Germany 52.0	Germany 63.5	International 39.0	Canada 69.7
Latvia 55.4	International 52.3	USA 55.8	Russian Federation 59.2	Ireland 64.4	England 74.2	Israel 51.9	Iceland 63.0	Romania 38.2	Ireland 69.6
Belgium (Fr) 55.4	Cyprus 51.9	International 55.5	Iceland 59.2	Denmark 64.3	Scotland 73.4	Scotland 51.6	Canada 63.0	England 37.1	Russian Federation 69.6
Australia 55.0	Germany 51.7	Lithuania 55.4	USA 58.5	Bulgaria 64.3	Denmark 72.3	France 50.8	Israel 63.0	Cyprus 36.9	Latvia 66.9
Lithuania 53.8	New Zealand 51.5	Norway 54.1	Israel 57.6	USA 62.7	Denmark 71.2	Belgium (Fr) 50.6	Spain 62.4	Israel 36.9	Thailand 66.1
Netherlands 53.5	Norway 51.2	Australia 53.5	International 57.0	Bulgaria 62.4	International 70.9	Russian Federation 50.0	Thailand 62.3	Norway 36.4	International 64.8
Norway 53.4	USA 49.3	Latvia 52.9	New Zealand 56.8	Iceland 61.6	Belgium (Fr) 70.2	Thailand 49.5	Thailand 62.3	Scotland 35.7	Belgium (Fr) 64.6
Greece 52.7	Scotland 49.3	Iceland 52.6	England 53.8	International 61.1	Germany 69.9	International 50.9	New Zealand 61.3	Denmark 35.5	Israel 63.3
USA 52.3	England 49.2	Greece 52.6	Denmark 51.9	Latvia 59.5	Lithuania 69.2	Greece 46.3	England 60.5	New Zealand 35.0	USA 62.5
Romania 52.3	Spain 49.2	Spain 50.6	Scotland 51.5	Israel 58.4	Israel 68.8	Denmark 46.0	Latvia 60.3	Iceland 33.6	Iceland 61.6
Denmark 51.0	Denmark 49.0	Portugal 49.9	Greece 51.3	Thailand 57.1	Bulgaria 68.1	Bulgaria 44.9	Romania 59.3	Iceland 33.1	Greece 59.4
Portugal 49.0	Latvia 47.3	New Zealand 49.3	Cyprus 50.9	Spain 54.8	Portugal 65.0	Spain 44.1	Greece 58.4	Spain 32.9	Spain 55.3
New Zealand 48.6	Greece 47.3	Denmark 48.8	Lithuania 49.0	Greece 54.5	Cyprus 64.4	Lithuania 42.3	Scotland 58.5	Lithuania 32.2	Lithuania 55.1
Iceland 48.4	Romania 47.0	Scotland 47.3	Spain 48.2	Lithuania 53.0	Greece 64.1	Cyprus 39.7	Cyprus 55.0	Spain 29.9	Portugal 54.9
Scotland 47.9	Iceland 44.4	Romania 46.9	Latvia 47.2	Portugal 50.7	Latvia 63.3	Latvia 38.9	Portugal 55.0	Greece 29.8	Bulgaria 52.8
England 46.8	Lithuania 39.1	England 45.9	Romania 45.8	Romania 46.4	Spain 62.2	Portugal 38.2	Lithuania 54.6	USA 27.8	Romania 50.0
Cyprus 45.8	Iran 37.9	Cyprus 43.5	Portugal 43.2	Cyprus 43.9	Romania 57.5	Romania 38.0	USA 53.0	Portugal 22.8	Cyprus 45.7
Iran 43.4	Portugal 34.8	Philippines 42.2	Philippines 35.7	Philippines 36.9	Philippines 49.2	Philippines 30.9	Iran 44.2	Iran 21.1	Philippines 36.0
Philippines 38.0	Philippines 30.0	Iran 33.7	Iran 35.3	Kuwait 34.7	Colombia 47.6	Colombia 28.7	Colombia 40.8	Kuwait 14.7	Iran 35.5
Colombia 34.2	Colombia 27.3	Colombia 31.9	Colombia 27.3	Colombia 33.8	Iran 46.3	Iran 27.0	Kuwait 35.7	Philippines 14.4	Kuwait 35.1
Kuwait 26.4	Kuwait 25.2	South Africa 28.3	South Africa 27.2	Iran 33.4	Kuwait 44.5	South Africa 20.3	Philippines 32.1	Colombia 11.9	Colombia 32.4
South Africa 26.0	South Africa 20.2	Kuwait 27.5	Kuwait 25.0	South Africa 28.6	Kuwait 36.8	Kuwait 20.2	South Africa 27.3	South Africa 8.3	South Africa 28.1

Promedio Internacional

Promedio EEUU

1995 TIMSS Ciencias 4º Grado – Porcentaje de respuestas correctas

Earth Features	Earth Processes	Earth in the Universe	Plants & Animals	Organs & Tissues	Life Processes & Functions	Life Cycles & Genetics	Interactions of Living Things
Korea 71	Korea 67	Czech Republic 75	Korea 81	Singapore 67	Korea 75	Netherlands 77	Netherlands 84
Japan 63	Japan 62	Hong Kong 75	Japan 78	Australia 66	Japan 75	Korea 75	USA 83
USA 60	USA 61	Hungary 75	Australia 72	Czech Republic 65	Netherlands 74	Czech Republic 73	Australia 82
England 59	Netherlands 58	Norway 75	Czech Republic 72	USA 65	Australia 70	Australia 71	Korea 82
Canada 58	Australia 56	Korea 74	Singapore 70	Hong Kong 65	Czech Republic 69	Japan 71	Japan 79
Czech Republic 58	England 55	Australia 72	USA 70	Korea 63	England 69	USA 70	Canada 77
Hungary 58	Canada 55	Canada 71	Netherlands 67	Japan 63	Singapore 69	Canada 69	Norway 76
Netherlands 57	Singapore 54	England 71	Canada 67	England 62	USA 68	Norway 68	England 76
Norway 56	Czech Republic 54	USA 70	England 67	New Zealand 61	Norway 67	England 68	Czech Republic 75
Australia 56	Hungary 53	Netherlands 69	Hungary 66	Canada 61	Canada 61	Hong Kong 68	Israel 75
New Zealand 54	New Zealand 53	Japan 69	Hong Kong 65	Hungary 61	Hungary 66	Hungary 67	Singapore 75
Hong Kong 54	International 50	Singapore 69	International 64	Netherlands 61	Hong Kong 66	Singapore 67	New Zealand 74
International 53	Hong Kong 51	International 67	Norway 60	Norway 61	Hungary 64	New Zealand 66	Hong Kong 74
Singapore 53	Israel 48	New Zealand 66	International 59	International 64	International 64	International 64	International 72
Israel 48	Thailand 45	Thailand 61	Israel 57	New Zealand 63	Thailand 48	Israel 62	Hungary 66
Thailand 42	Norway 42	Israel 58	Thailand 56	Thailand 55	Thailand 53	Thailand 53	Thailand 53

Human Biology & Health	Matter	Energy & Physical	Physical & Chemical	Forces & Motion	Environmental & Resource	Scientific Processes
Netherlands 72	Korea 77	Korea 73	Netherlands 74	Korea 68	Korea 74	Korea 66
Korea 70	Japan 75	Japan 70	Korea 72	Japan 62	Japan 72	USA 63
Australia 70	Netherlands 68	Australia 63	Japan 72	Czech Republic 62	Australia 69	Australia 59
USA 69	Singapore 67	Netherlands 62	Hong Kong 68	Netherlands 61	USA 68	Singapore 54
Norway 68	Australia 63	England 62	Czech Republic 67	Singapore 60	Netherlands 65	England 54
Singapore 68	USA 61	Canada 61	USA 65	Norway 58	Czech Republic 63	Japan 53
England 67	Canada 61	Czech Republic 61	Singapore 65	Canada 56	Hungary 62	Netherlands 52
Hong Kong 67	Czech Republic 61	USA 61	Australia 63	Australia 55	Canada 61	New Zealand 52
Canada 66	Hong Kong 60	Singapore 61	Canada 62	Hungary 55	England 60	Hong Kong 51
Czech Republic 66	Hungary 59	Hong Kong 59	England 61	Hong Kong 54	New Zealand 59	Czech Republic 51
Japan 66	England 58	Israel 58	Hungary 60	USA 53	International 58	Canada 51
Hungary 65	International 58	Hungary 57	International 59	New Zealand 52	Norway 58	Israel 50
New Zealand 64	New Zealand 58	International 56	Norway 58	International 51	Israel 58	Norway 48
International 63	Norway 56	New Zealand 56	Israel 57	England 49	Singapore 57	International 46
Israel 62	Israel 53	Norway 53	New Zealand 57	Thailand 47	Hong Kong 54	Hungary 40
Thailand 52	Thailand 46	Thailand 44	Thailand 46	Israel 46	Thailand 53	Thailand 40

1995 TIMSS Ciencias grado 8º – Porcentaje de respuestas correctas

Earth Features		Earth Processes		Earth in the Universe		Diversity & Structure of Living Things		Life Processes & Functions		Life Cycles & Genetics		Interactions of Living Things		Human Biology & Health		Properties & Classification of Matter	
Czech Republic	67	England	67	Sweden	71	Japan	76	Singapore	72	Czech Republic	82	Korea	69	Singapore	74	Japan	67
Hungary	67	Singapore	67	Norway	70	Singapore	74	Japan	70	USA	81	Singapore	66	Czech Republic	72	Singapore	67
Korea	65	Belgium (Fl)	65	Netherlands	67	Hong Kong	73	Korea	68	England	80	Japan	65	Netherlands	71	Korea	65
Singapore	65	Netherlands	62	Czech Republic	67	Korea	72	Czech Republic	64	Netherlands	79	Thailand	64	Japan	69	Czech Republic	60
Belgium (Fl)	61	Norway	62	Japan	67	Czech Republic	72	Thailand	63	Israel	79	Hungary	63	Belgium (Fl)	69	Netherlands	58
Sweden	61	Thailand	66	Netherlands	72	Netherlands	63	Belgium (Fl)	63	Belgium (Fl)	79	Australia	62	Hungary	69	Belgium (Fl)	58
Thailand	60	Singapore	65	Thailand	69	Thailand	61	Netherlands	61	Canada	78	England	62	England	68	Hungary	57
Russian Federation	61	Switzerland	65	Sweden	68	Hungary	60	Hungary	60	Sweden	78	Norway	60	Israel	68	Sweden	57
Russian Federation	59	Canada	61	Sweden	60	Hungary	67	Russian Federation	59	Russia Federation	76	Canada	58	Germany	68	Hong Kong	56
Norway	59	Korea	64	Korea	59	Australia	63	England	59	Korea	76	Czech Republic	58	USA	67	Canada	56
Japan	59	USA	63	Australia	67	Germany	66	Germany	58	France	76	New Zealand	56	Thailand	67	Norway	55
England	59	Japan	58	Germany	63	Russian Federation	66	USA	58	Russian Federation	76	Netherlands	56	Australia	66	Australia	55
Switzerland	58	New Zealand	57	Spain	63	England	64	Australia	57	Germany	75	USA	54	Korea	66	England	55
Netherlands	58	Czech Republic	57	Australia	63	USA	64	Canada	57	Switzerland	75	Germany	53	Canada	65	Germany	55
Australia	57	Australia	57	Belgium (Fl)	62	Canada	63	Israel	57	Japan	75	Belgium (Fl)	53	Sweden	64	Russian Federation	54
Germany	57	Thailand	56	New Zealand	62	Canada	61	Hong Kong	56	New Zealand	74	Spain	53	New Zealand	64	New Zealand	54
USA	57	Switzerland	56	Canada	61	Belgium (Fl)	63	New Zealand	56	Hungary	74	Russian Federation	52	Spain	63	Israel	53
Canada	57	Spain	55	England	59	New Zealand	62	New Zealand	56	Australia	73	Sweden	52	Russian Federation	63	France	52
Israel	56	France	55	Hungary	59	Spain	61	Spain	56	Spain	71	International	51	Norway	63	International	52
Spain	56	Israel	55	International	58	International	61	Sweden	55	International	70	Israel	50	Switzerland	61	Switzerland	51
New Zealand	56	Germany	54	Hong Kong	58	Switzerland	61	International	55	Singapore	69	Switzerland	50	International	61	USA	50
International	55	International	54	Israel	56	Israel	60	Switzerland	54	Thailand	67	Hong Kong	47	Hong Kong	60	Spain	50
France	55	Hong Kong	52	Norway	59	Norway	54	Norway	54	Hong Kong	65	France	45	France	56	Thailand	47
Hong Kong	54	Hungary	51	France	53	France	58	France	54	Thailand	56	Russian Federation	40	Russian Federation	47	Spain	50

Structure of Matter		Energy & Physical Processes		Physical Changes		Chemical Changes		Forces & Motion		Science, Technology, & Society		Environmental & Resource Issues		Scientific Processes			
Russian Federation	56	Singapore	71	Japan	67	Singapore	74	Czech Republic	78	Korea	74	Singapore	73	Singapore	75		
Hungary	54	Japan	69	Singapore	63	Korea	66	Japan	74	Hungary	73	Thailand	70	Korea	64		
Czech Republic	54	Korea	67	Czech Republic	63	Hungary	65	Singapore	73	Netherlands	67	England	67	Netherlands	65		
Singapore	53	England	64	France	62	Czech Republic	64	Netherlands	71	Sweden	67	Australia	65	France	62		
Spain	51	Netherlands	64	Israel	61	England	64	Korea	70	Singapore	66	Netherlands	65	Czech Republic	61		
USA	48	Czech Republic	62	Sweden	61	Japan	64	Hong Kong	69	Belgium (Fl)	65	Korea	63	Australia	61		
Israel	45	Belgium (Fl)	62	Netherlands	61	Australia	62	Switzerland	69	New Zealand	60	Japan	62	Japan	60		
Sweden	43	Australia	61	Hungary	61	Russian Federation	62	Hungary	69	USA	61	Canada	61	England	60		
Korea	42	Hungary	60	Norway	60	England	59	England	68	England	57	New Zealand	61	Canada	59		
Japan	41	New Zealand	60	Belgium (Fl)	59	Germany	61	Sweden	68	England	57	England	61	USA	59		
Hong Kong	40	Canada	60	Canada	59	Israel	61	Australia	67	Hong Kong	55	Canada	53	Belgium (Fl)	60	Hungary	57
International	40	Hong Kong	60	Canada	59	Canada	60	Norway	67	Canada	53	Switzerland	53	Czech Republic	59	Hong Kong	57
Australia	39	Israel	59	Korea	57	New Zealand	59	Canada	66	Canada	53	Spain	59	Spain	57	New Zealand	57
England	38	Germany	59	Australia	57	Hong Kong	58	Germany	67	Norway	52	Norway	58	Czech Republic	52	Thailand	55
Canada	37	Switzerland	59	Russian Federation	57	Spain	58	New Zealand	66	Czech Republic	52	Australia	52	International	53	Germany	53
Germany	35	Russian Federation	58	Switzerland	54	Netherlands	58	Belgium (Fl)	65	Israel	51	Sweden	52	International	53	Israel	52
New Zealand	35	USA	57	Germany	54	Sweden	57	France	64	France	48	International	48	Israel	52	Switzerland	53
Norway	32	Norway	57	Thailand	53	International	56	Spain	63	USA	48	USA	50	Switzerland	50	International	53
Thailand	31	Sweden	57	Spain	53	Belgium (Fl)	56	Russian Federation	62	Germany	47	Germany	50	Sweden	52	Norway	52
Netherlands	30	International	56	International	53	Switzerland	55	Norway	53	International	61	Spain	44	France	49	Russian Federation	51
France	29	Thailand	55	New Zealand	53	France	53	Israel	55	Israel	43	France	49	Russian Federation	47	Spain	50
Switzerland	29	Spain	55	USA	49	Thailand	51	Thailand	56	Russian Federation	40	Russian Federation	47				
Belgium (Fl)	27	France	55	Hong Kong	49												

Desempeño en tópicos específicos en matemáticas 1995 TIMSS

Whole Numbers	Common Fractions	Decimal Fractions & Percentages	Relationships of Fractions	Estimations of Quantity/Size	Rounding	Estimating Computations	Measurement Units	Perimeter, Area, Volume	Measurement Estimations & Errors
Singapore 80.4	Singapore 82.4	Singapore 77.9	Singapore 85.1	Japan 77.9	Czech Republic 86.9	Singapore 75.8	Singapore 77.9	Singapore 84.5	Czech Republic 82.9
Japan 72.0	Japan 72.2	Czech Republic 72.5	Korea 77.6	Singapore 77.3	Singapore 86.6	Czech Republic 69.8	Japan 74.8	Japan 72.6	Singapore 81.0
Switzerland 70.2	Korea 69.9	Hong Kong 71.1	Japan 75.3	England 72.2	Canada 84.7	Japan 69.0	Czech Republic 73.2	Hong Kong 63.9	Sweden 80.8
Belgium (Fl) 68.6	Hong Kong 69.4	Japan 69.8	Hong Kong 74.1	Hong Kong 71.8	Korea 83.8	Korea 66.7	Slovenia 72.0	Korea 61.8	Korea 79.5
Austria 68.4	Belgium (Fl) 68.7	Slovak Republic 69.1	Belgium (Fl) 71.3	Switzerland 71.8	Iceland 83.1	Belgium (Fl) 64.1	Slovak Republic 71.9	Austria 50.4	Belgium (Fl) 78.9
Korea 67.6	Switzerland 62.4	Hungary 68.7	Switzerland 70.0	Czech Republic 71.7	Slovak Republic 82.4	Switzerland 62.5	Belgium (Fl) 71.8	Czech Republic 48.9	Hungary 78.2
Czech Republic 67.4	Ireland 61.7	Korea 68.4	France 67.2	Netherlands 71.2	Belgium (Fl) 81.0	Canada 61.3	Switzerland 71.6	Slovak Republic 47.9	Switzerland 78.2
Hong Kong 65.4	Austria 60.4	Austria 66.6	Austria 66.8	Belgium (Fl) 70.7	Hungary 79.8	Slovak Republic 61.1	Sweden 69.5	Austria 47.9	Austria 77.7
Slovak Republic 64.6	Belgium (Fr) 59.8	Russian Federation 65.9	Belgium (Fr) 65.8	Korea 70.7	Japan 79.6	Ireland 60.5	France 69.0	Slovenia 45.8	Netherlands 76.1
France 64.5	Slovenia 59.7	France 64.9	Canada 65.1	Austria 69.9	USA 79.2	Sweden 60.0	Austria 68.1	Belgium (Fr) 45.6	France 75.2
Slovenia 63.4	Czech Republic 59.6	Belgium (Fl) 64.6	Czech Republic 64.9	Australia 69.3	Netherlands 78.5	Australia 59.1	Bulgaria 68.1	Bulgaria 45.2	Slovak Republic 75.2
Russian Federation 62.7	Netherlands 58.9	Slovenia 62.9	Ireland 64.3	Hungary 69.3	Sweden 78.5	Austria 58.9	Ireland 68.1	Russian Federation 44.6	Australia 74.5
Bulgaria 62.5	Slovak Republic 58.6	Switzerland 61.9	Slovak Republic 63.0	Sweden 69.3	Australia 77.5	Netherlands 58.7	Bulgaria 68.0	France 44.1	Norway 74.5
Ireland 62.2	France 57.8	Canada 61.0	Germany 62.6	Slovak Republic 69.1	Switzerland 77.4	Hong Kong 57.8	Korea 67.9	Netherlands 44.0	Denmark 73.0
Spain 60.8	Hungary 57.7	Sweden 59.2	Netherlands 62.5	France 69.0	Ireland 76.5	New Zealand 57.6	Hungary 67.5	Belgium (Fr) 43.0	Germany 72.9
Hungary 60.6	Israel 57.4	Belgium (Fr) 58.6	Slovenia 62.4	Germany 69.0	Austria 75.9	Hungary 57.3	Netherlands 66.8	Hungary 42.9	Hong Kong 72.7
Sweden 58.9	Canada 56.2	Thailand 58.0	Sweden 62.2	Canada 67.8	Thailand 75.4	Norway 57.0	Norway 66.4	Australia 42.1	Japan 72.5
Canada 57.9	Russian Federation 55.8	Netherlands 57.8	Australia 61.0	Scotland 68.8	France 74.7	USA 55.7	Russian Federation 65.9	Canada 40.4	Slovenia 72.5
Israel 59.0	Australia 55.4	Bulgaria 57.8	Hungary 60.7	Norway 66.6	Slovenia 74.7	Iceland 54.7	Denmark 65.4	Thailand 40.0	England 71.8
Thailand 56.0	Thailand 54.2	Ireland 57.3	Bulgaria 59.9	Belgium (Fr) 65.8	New Zealand 74.4	England 54.4	Hong Kong 65.2	Ireland 39.4	New Zealand 70.6
International 55.7	Bulgaria 54.2	Germany 57.2	Thailand 59.6	Slovenia 65.5	Hong Kong 74.2	Slovenia 52.6	Australia 65.0	Sweden 39.3	Scotland 69.9
International 55.7	Bulgaria 53.1	Israel 56.3	Norway 59.6	New Zealand 65.3	Russian Federation 73.5	Germany 52.0	International 39.0	International 39.0	Canada 69.7
Germany 55.4	International 52.3	USA 55.8	Russian Federation 59.2	Ireland 64.4	England 74.2	Israel 51.9	Iceland 63.0	Romania 38.2	Ireland 69.6
Latvia 55.4	International 52.3	USA 55.8	Iceland 59.2	Denmark 64.3	Scotland 73.4	Scotland 51.6	Canada 63.0	England 37.1	Russian Federation 69.6
Belgium (Fr) 55.4	Cyprus 51.9	International 55.5	USA 58.5	Russian Federation 63.5	Norway 72.3	France 50.8	Israel 63.0	Cyprus 36.9	Latvia 66.9
Australia 55.0	Germany 51.7	Lithuania 55.4	Israel 57.6	USA 62.7	Denmark 71.2	Belgium (Fr) 50.6	Spain 62.4	Israel 36.9	Thailand 66.1
Lithuania 53.8	New Zealand 51.5	Norway 54.1	International 57.0	Bulgaria 62.4	International 70.9	Russian Federation 50.0	Thailand 62.3	Norway 36.4	International 64.8
Netherlands 53.5	Norway 51.2	Australia 53.5	New Zealand 56.8	Iceland 61.6	Belgium (Fr) 70.2	Thailand 49.5	International 61.6	Scotland 35.7	Belgium (Fr) 64.6
Norway 53.4	USA 49.3	Latvia 52.9	England 53.8	International 61.1	Germany 69.9	International 50.9	New Zealand 61.3	Denmark 35.5	Israel 63.3
Greece 52.7	Scotland 49.3	Iceland 52.6	Denmark 51.9	Latvia 59.5	Lithuania 69.2	Greece 46.3	England 60.5	New Zealand 35.0	USA 62.5
USA 52.3	England 49.2	Greece 52.6	Scotland 51.5	Israel 58.4	Israel 68.8	Denmark 46.0	Latvia 60.3	Latvia 33.6	Iceland 61.6
Romania 52.3	Spain 49.2	Spain 50.6	Greece 51.3	Thailand 57.1	Bulgaria 68.1	Bulgaria 44.9	Romania 59.3	Iceland 33.1	Greece 59.4
Denmark 51.0	Denmark 49.0	Portugal 49.9	Greece 51.3	Portugal 65.0	Spain 64.1	Greece 44.1	Greece 58.4	Germany 32.9	Spain 55.3
Portugal 49.0	Latvia 47.3	New Zealand 49.3	Cyprus 50.9	Spain 54.8	Cyprus 64.4	Lithuania 42.3	Scotland 58.5	Lithuania 32.2	Lithuania 55.1
New Zealand 48.6	Greece 47.3	Denmark 48.8	Lithuania 49.0	Greece 54.5	Greece 64.1	Cyprus 39.7	Cyprus 55.0	Spain 29.9	Portugal 54.9
Iceland 48.4	Romania 47.0	Scotland 47.3	Spain 48.2	Lithuania 53.0	Latvia 63.3	Latvia 38.9	Portugal 55.0	Bulgaria 29.8	Bulgaria 52.8
Scotland 47.9	Iceland 44.4	Romania 46.9	Latvia 47.2	Portugal 50.7	Spain 62.2	Portugal 38.2	Lithuania 54.6	Greece 29.8	Romania 50.0
England 46.8	Lithuania 39.1	England 45.9	Romania 45.8	Romania 46.4	Romania 57.5	Romania 38.0	USA 53.0	Portugal 22.8	Cyprus 45.7
Cyprus 45.8	Iran 37.9	Cyprus 43.5	Portugal 43.2	Cyprus 43.9	Philippines 36.9	Philippines 30.9	Iran 44.2	Iran 21.1	Philippines 36.0
Iran 43.4	Portugal 34.8	Philippines 42.2	Philippines 35.7	Philippines 36.9	Philippines 49.2	Philippines 30.9	Kuwait 14.7	Kuwait 35.5	Kuwait 35.1
Philippines 38.0	Philippines 30.0	Iran 33.7	Iran 35.3	Kuwait 34.7	Colombia 47.6	Colombia 28.7	Colombia 40.8	Philippines 14.4	Colombia 32.3
Colombia 34.2	Colombia 27.3	Colombia 31.9	Colombia 27.3	Colombia 33.8	Iran 46.3	Iran 27.0	Kuwait 35.7	Kuwait 35.1	Colombia 32.3
Kuwait 26.4	Kuwait 25.2	South Africa 28.3	South Africa 27.2	Iran 33.4	Kuwait 44.5	South Africa 20.3	Philippines 32.1	South Africa 27.3	South Africa 28.1
South Africa 26.0	South Africa 20.2	Kuwait 27.5	Kuwait 25.0	South Africa 28.6	South Africa 36.8	Kuwait 20.2	South Africa 27.3	South Africa 8.3	South Africa 28.1

Promedio Internacional

Promedio COLOMBIA

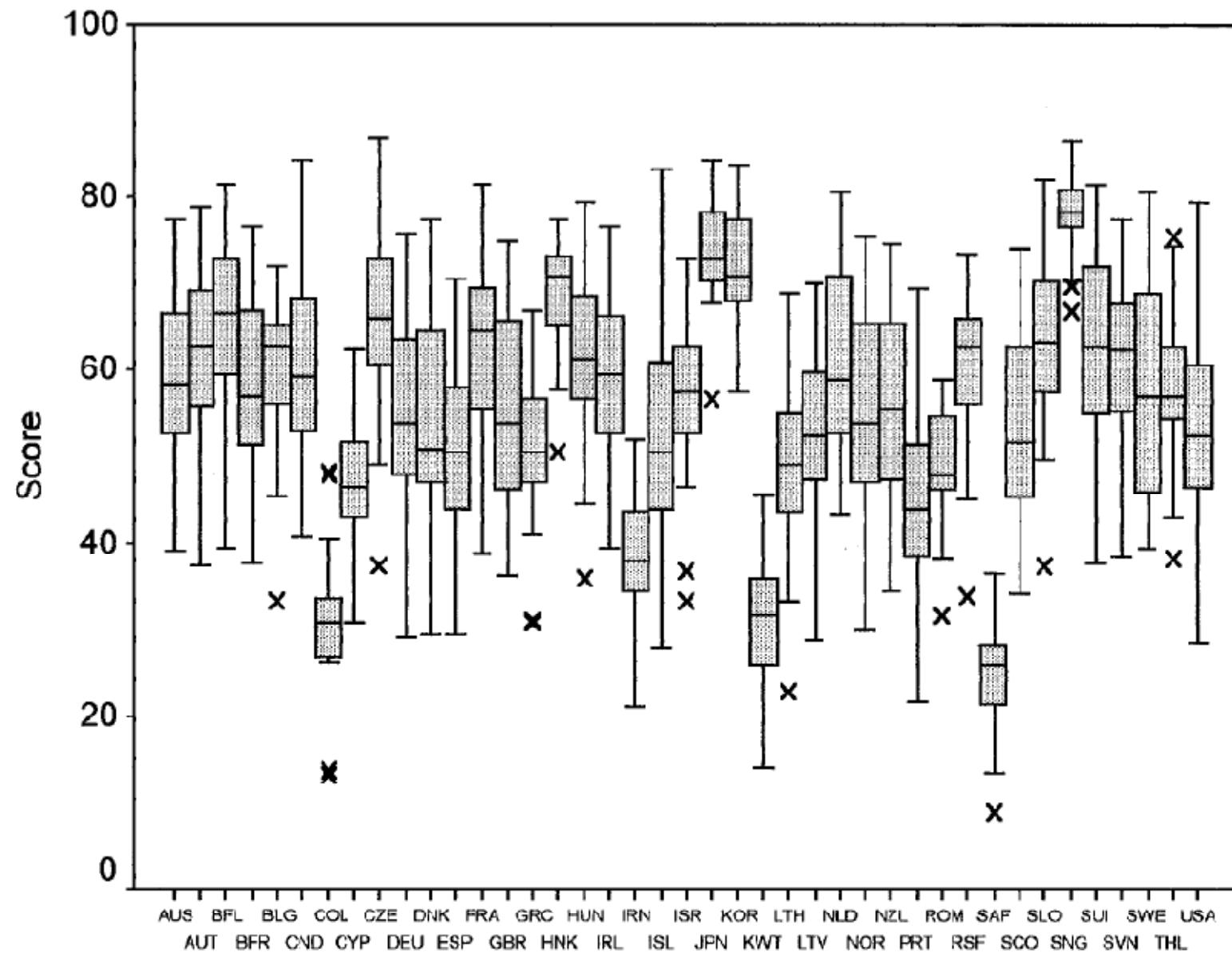
Desempeño en tópicos específicos en matemáticas 1995 TIMSS

2D Geo. Basics	Polygons & Circles	3D Geo. & Transformations	Congruence & Similarity	Proportionality Concepts	Proportionality Problems	Patterns, Relations & Functions	Equations & Formulas	Data Representation & Analysis	Statistics & Probability
Japan 78.9	Korea 73.0	Japan 84.3	Japan 79.7	Singapore 70.1	Singapore 76.7	Japan 70.0	Singapore 79.8	Japan 84.3	Singapore 78.5
Singapore 78.3	Japan 70.8	Singapore 78.6	Korea 76.9	Korea 57.0	Japan 67.8	Korea 68.4	Japan 72.3	Korea 81.9	Korea 77.8
Korea 75.5	Singapore 70.6	Czech Republic 77.7	Singapore 76.7	Japan 56.9	Korea 65.1	Singapore 67.2	Hong Kong 70.5	France 81.4	Belgium (Fl) 77.7
Hong Kong 73.5	Hong Kong 65.4	France 77.7	Hong Kong 71.0	Hong Kong 50.1	Hong Kong 64.0	Hong Kong 60.8	Korea 70.0	Switzerland 81.3	Japan 75.0
Russian Federation 63.4	Belgium (Fl) 64.1	Hong Kong 77.6	France 69.7	Netherlands 41.9	Czech Republic 61.3	Czech Republic 60.2	Czech Republic 64.3	Singapore 81.0	Hong Kong 73.0
Netherlands 62.9	Bulgaria 63.4	Switzerland 75.9	Czech Republic 66.1	Ireland 41.2	Belgium (Fl) 59.4	England 60.1	Belgium (Fl) 62.1	Netherlands 80.6	Netherlands 72.4
Thailand 62.4	France 61.9	Slovak Republic 75.2	Bulgaria 66.0	Canada 40.3	Slovak Republic 58.7	Switzerland 59.5	Russian Federation 61.4	Czech Republic 79.6	Switzerland 72.4
Czech Republic 62.1	Israel 59.7	Belgium (Fr) 74.5	Slovak Republic 63.2	Sweden 39.2	Bulgaria 58.3	Bulgaria 59.2	Hungary 60.9	Sweden 79.5	Ireland 70.3
Bulgaria 61.7	Czech Republic 57.4	Belgium (Fl) 73.7	Thailand 62.7	Belgium (Fl) 39.0	Switzerland 57.3	Slovak Republic 59.1	Slovak Republic 60.6	Belgium (Fl) 79.5	Canada 70.0
Hungary 61.6	Romania 57.3	Korea 73.3	Russian Federation 62.3	Slovenia 38.1	Russian Federation 56.3	Canada 58.2	Slovenia 60.1	Austria 78.7	Sweden 68.7
Slovak Republic 59.8	Russian Federation 57.2	Bulgaria 72.6	Belgium (Fl) 57.5	Australia 37.8	Thailand 56.0	Australia 57.6	Bulgaria 59.4	Denmark 77.6	Belgium (Fr) 68.5
Australia 58.8	Belgium (Fr) 54.2	Hungary 71.0	Latvia 56.9	France 37.3	Hungary 55.9	Austria 56.3	Israel 58.3	Slovenia 77.5	Australia 67.5
Belgium (Fl) 58.8	Thailand 53.5	Netherlands 70.6	Slovenia 56.6	Switzerland 36.8	Netherlands 55.9	Netherlands 56.9	Austria 58.2	Belgium (Fr) 76.8	France 66.5
Slovenia 58.3	Slovak Republic 53.2	Slovenia 70.2	Romania 56.1	Czech Republic 37.3	Belgium (Fr) 55.9	Scotland 56.5	Thailand 54.0	Hong Kong 76.4	Hungary 66.2
Austria 58.1	Slovenia 53.2	Russian Federation 70.2	Israel 54.8	Austria 36.5	France 55.7	New Zealand 55.7	France 53.6	Ireland 76.2	New Zealand 65.9
Switzerland 57.9	Hungary 51.6	Canada 70.1	Lithuania 53.8	Thailand 36.5	Slovenia 55.3	Ireland 55.5	Belgium (Fr) 52.8	Germany 76.0	England 65.3
France 56.1	Canada 50.5	Austria 69.5	Hungary 53.4	Belgium (Fr) 36.1	Austria 55.2	Slovenia 55.4	Australia 52.8	Norway 75.5	Norway 64.7
New Zealand 55.8	Australia 50.4	New Zealand 67.3	Slovak Republic 35.9	Ireland 52.4	Ireland 52.4	France 55.0	Ireland 52.7	Slovak Republic 75.2	Austria 64.6
England 54.9	Greece 49.6	Latvia 66.6	England 34.8	Australia 52.2	Slovak Republic 54.3	Canada 52.4	Spain 52.2	Australia 75.2	Slovenia 63.7
Canada 54.7	Latvia 49.1	England 66.3	Hungary 34.6	Canada 51.6	Bulgaria 53.7	Spain 52.2	Canada 75.0	Czech Republic 63.4	USA 63.1
International 53.7	International 48.9	Australia 65.5	Belgium (Fr) 51.9	International 33.6	International 50.2	Thailand 53.4	Switzerland 51.9	England 74.8	USA 63.1
Denmark 53.9	Austria 48.7	Denmark 65.4	Switzerland 51.2	International 33.6	International 50.2	Thailand 53.4	Switzerland 51.9	Thailand 74.5	Scotland 62.4
Latvia 53.3	Switzerland 48.6	International 63.4	Cyprus 51.1	Russian Federation 33.5	Sweden 49.2	Russian Federation 53.2	Netherlands 51.7	Scotland 74.2	Germany 62.4
Scotland 52.6	Ireland 48.0	Israel 64.8	Australia 50.9	New Zealand 33.4	Germany 49.0	Israel 53.2	International 50.7	International 50.7	International 50.7
Israel 52.5	England 47.0	Thailand 64.5	Denmark 50.3	Scotland 32.4	Latvia 48.2	International 51.5	Romania 50.5	New Zealand 74.1	Israel 62.3
Ireland 52.4	Cyprus 46.7	Germany 63.7	Netherlands 51.0	USA 31.5	Denmark 47.7	USA 51.1	USA 49.4	Hungary 73.7	Iceland 62.0
Norway 52.1	Lithuania 44.6	Lithuania 63.7	Austria 48.9	Israel 31.4	England 47.2	Spain 50.3	Latvia 49.1	Israel 73.2	Denmark 61.9
Belgium (Fr) 51.4	Iceland 44.3	Scotland 63.2	Iceland 48.5	Romania 31.3	New Zealand 47.1	Belgium (Fr) 49.9	Cyprus 46.7	Iceland 72.6	Bulgaria 61.1
Spain 49.5	Germany 44.3	Iceland 60.4	Greece 48.2	Norway 30.9	Norway 47.1	Norway 48.7	New Zealand 46.6	USA 72.6	International 59.9
Germany 49.3	Netherlands 44.0	Greece 58.8	Norway 46.9	Bulgaria 30.6	Romania 46.7	Denmark 48.6	Germany 46.4	Russian Federation 72.0	Spain 58.0
Lithuania 48.9	New Zealand 43.2	Norway 58.6	Ireland 46.7	Greece 29.6	Israel 46.5	Germany 47.6	Greece 45.6	International 71.0	Russian Federation 56.9
Iceland 48.7	Scotland 42.8	USA 58.4	Sweden 45.9	Iceland 29.4	Scotland 45.4	Sweden 47.2	Lithuania 45.3	Bulgaria 70.8	Cyprus 57.2
Greece 48.6	Sweden 42.8	Spain 58.2	Scotland 45.6	Denmark 28.8	USA 45.2	Latvia 47.2	Norway 44.9	Spain 70.4	Slovak Republic 57.0
USA 47.9	Norway 42.4	Ireland 57.8	England 45.6	Spain 27.4	Iceland 44.6	Iceland 44.7	Portugal 67.0	Latvia 70.0	Thailand 56.5
Romania 47.5	Denmark 40.1	Sweden 55.9	Germany 45.1	Latvia 27.3	Spain 43.6	Romania 45.4	Denmark 44.0	Portugal 69.7	Greece 52.6
Sweden 46.1	Spain 39.3	Portugal 51.9	Iran 44.1	Germany 26.5	Cyprus 43.3	Portugal 45.3	Sweden 43.7	Lithuania 67.0	Latvia 51.6
Cyprus 43.8	USA 39.1	Romania 50.7	Iran 44.1	Iran 22.9	Greece 41.1	Lithuania 45.2	Greece 42.5	Greece 66.6	Romania 46.7
Portugal 42.8	Iran 37.9	Cyprus 49.9	Spain 43.6	Lithuania 21.8	Portugal 41.0	Cyprus 42.3	Portugal 36.6	Romania 58.0	Lithuania 43.6
Iran 41.8	Portugal 35.5	Iran 47.3	Portugal 43.2	Portugal 20.3	Iran 38.0	Cyprus 41.7	Iran 35.6	Iran 52.0	Iran 36.4
Kuwait 35.4	Kuwait 31.3	Kuwait 44.2	Kuwait 38.2	Philippines 17.1	Philippines 32.8	Colombia 33.2	Kuwait 29.5	Colombia 47.7	Kuwait 34.8
Philippines 32.1	Colombia 27.8	Philippines 36.5	Philippines 31.4	Kuwait 13.7	Colombia 29.8	Philippines 33.1	Philippines 29.4	Philippines 45.9	Philippines 32.6
Colombia 27.0	Philippines 27.3	Colombia 36.4	Colombia 26.5	Colombia 13.0	Kuwait 29.5	Kuwait 32.6	Colombia 24.5	Kuwait 45.8	Colombia 31.3
South Africa 25.7	South Africa 21.7	South Africa 26.1	South Africa 23.2	South Africa 11.9	South Africa 27.0	South Africa 20.4	South Africa 22.9	South Africa 29.4	South Africa 28.1

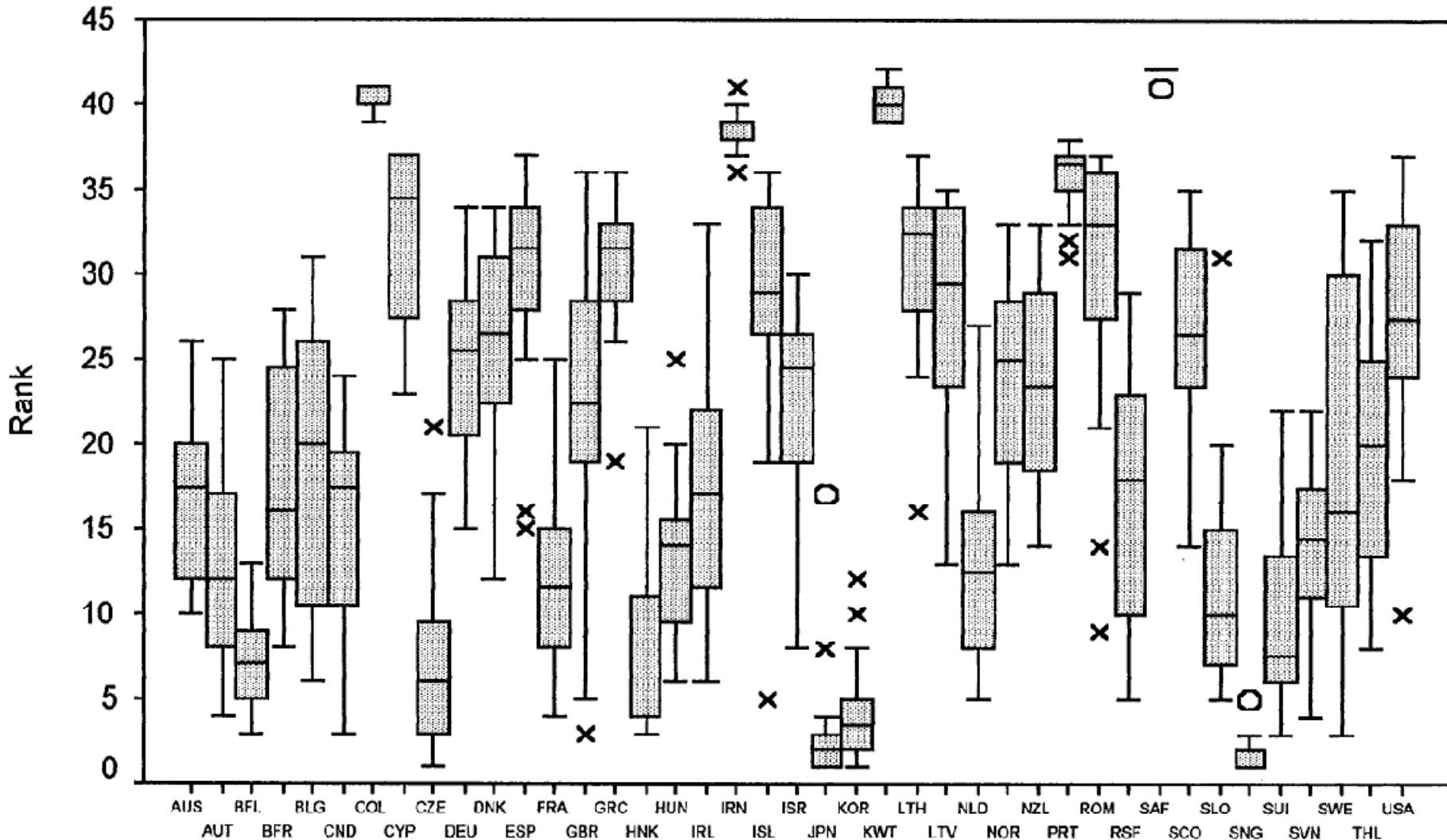
Promedio Internacional

Promedio COLOMBIA

Distribución de los resultados en matemáticas 8º grado por país



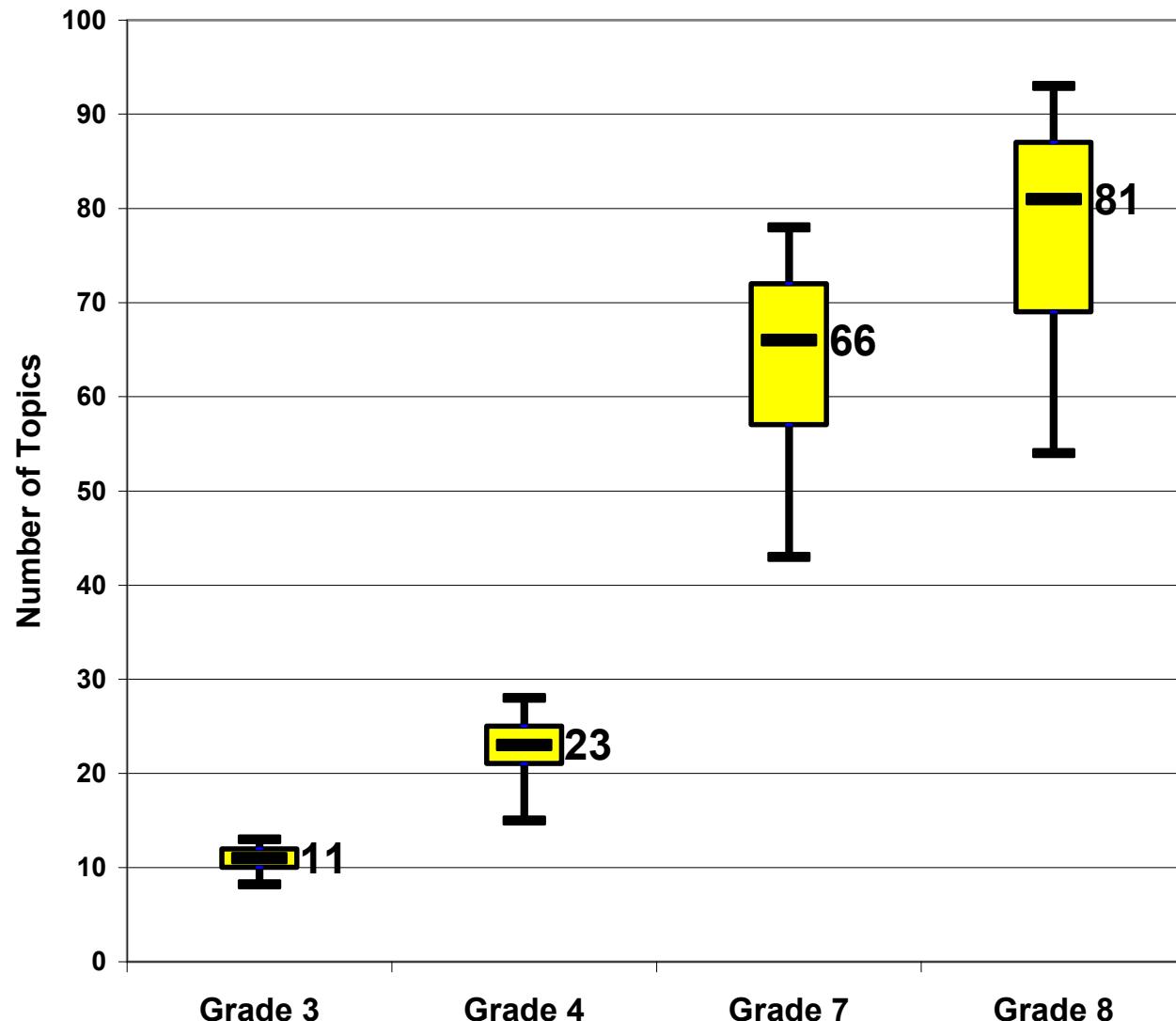
Distribución de los ranks de los países en matemáticas 8º grado



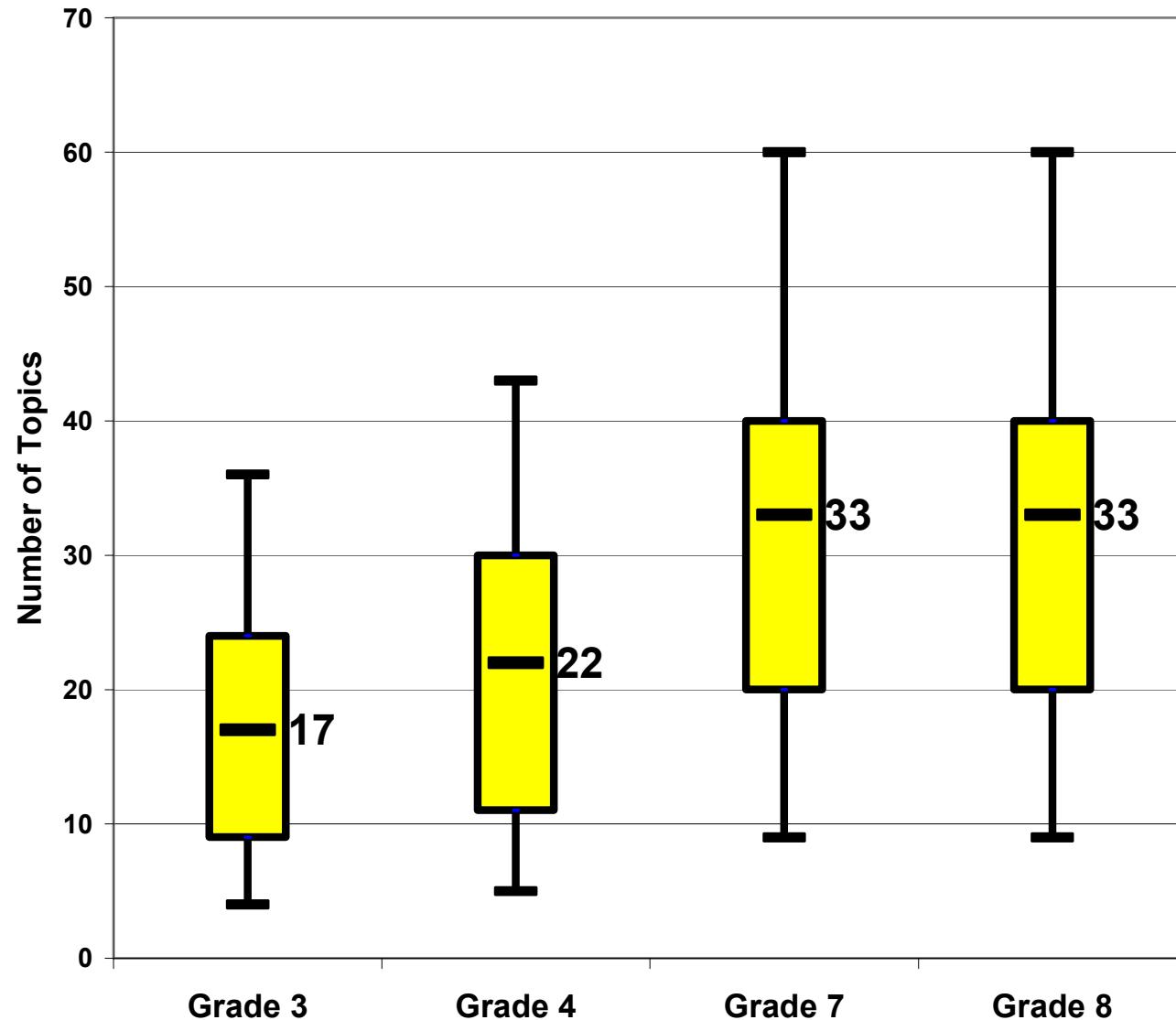
Alineación con escenario ideal

Países	Número de tópicos en currículo	Número de tópicos desalineados	Número de tópicos alineados	Número de tópicos desalineados
Argentina	81	3	54	24
Australia	136	32	75	29
Belgium (Fl)	155	37	87	31
Canada	181	58	92	31
Cyprus	162	49	87	26
Czech Republic	119	32	83	4
France	156	40	85	31
Germany	117	33	74	10
Hong Kong	79	9	62	8
Hungary	158	49	93	16
Iceland	137	32	81	24
Japan	128	39	86	3
Korea	125	27	90	8
Netherlands	97	14	54	29
Norway	159	33	96	30
Portugal	144	48	84	12
Singapore	115	11	84	21
Spain	109	23	69	17
USA	186	63	98	25

Número de tópicos alineados con escenario ideal



Número de tópicos no alineados (Introducidos antes del escenario ideal)



Análisis de regresión de logro contra coherencia y medida de foco

<i>Model</i>	<i>Grade 3</i>	<i>Grade 4</i>	<i>Grade 7</i>	<i>Grade 8</i>
<i>Predictor</i>	Estimate (StdError, p)			
<i>Number of Topics Aligned with Ideal Scenario</i>	9.94 (7.38 , 0.196)	7.48 (4.04 , 0.081)	3.57 (1.48 , 0.023)	2.83 (1.12 , 0.017)
<i>Total Number of Topics in Curriculum</i>	-2.42 (1.13 , 0.047)	-2.58 (1.05 , 0.025)	-1.64 (0.57 , 0.008)	-1.39 (0.45 , 0.004)
<i>Model Fit</i>				
<i>R-Square</i>	0.2191	0.2574	0.2205	0.2490
<i>Residual Mean Sq.</i>	1652.9	1489.0	1476.0	1331.4
<i>p<</i>	0.1222	0.0687	0.0270	0.0136
<i>No. of Countries</i>	20	21	32	33
<i>Standardized Coefficient</i>				
<i>Number of Topics Aligned with Ideal Scenario</i>	0.4374	0.7331	0.8481	0.8240
<i>Total Number of Topics in Curriculum</i>	-0.6969	-0.9703	-1.0044	-1.0204

Puntaje grado 8 en matemáticas vs. Tasa de número de tópicos alineados / total de tópicos en el currículo

